



From lab to production,  
providing a window into the process



# Practical Rheology

## LCR 7001 Capillary Rheometer

Azadeh Farahanchi  
Rheological Scientist

38 Forge Parkway, Franklin, MA 02038

Tel: 508.541.9582

Cell: 774.287.2366

[Azadeh.Farahanchi@dynisco.com](mailto:Azadeh.Farahanchi@dynisco.com)

Proprietary & Confidential



# Outline

1. Introduction
2. Shear Sweep Test (Polymer Flow Behavior )
3. Rabinowicz and Bagley Corrections
4. Extensional Viscosity Measurements
5. Wall Slip Velocity Calculation
6. Time Sweep Test (Thermal Stability of Polymers )
7. Die Swell Measurements
8. MFR Correlation
9. Intrinsic Viscosity of PET
10. LCR Dies Information



*From lab to production,  
providing a window into the process*

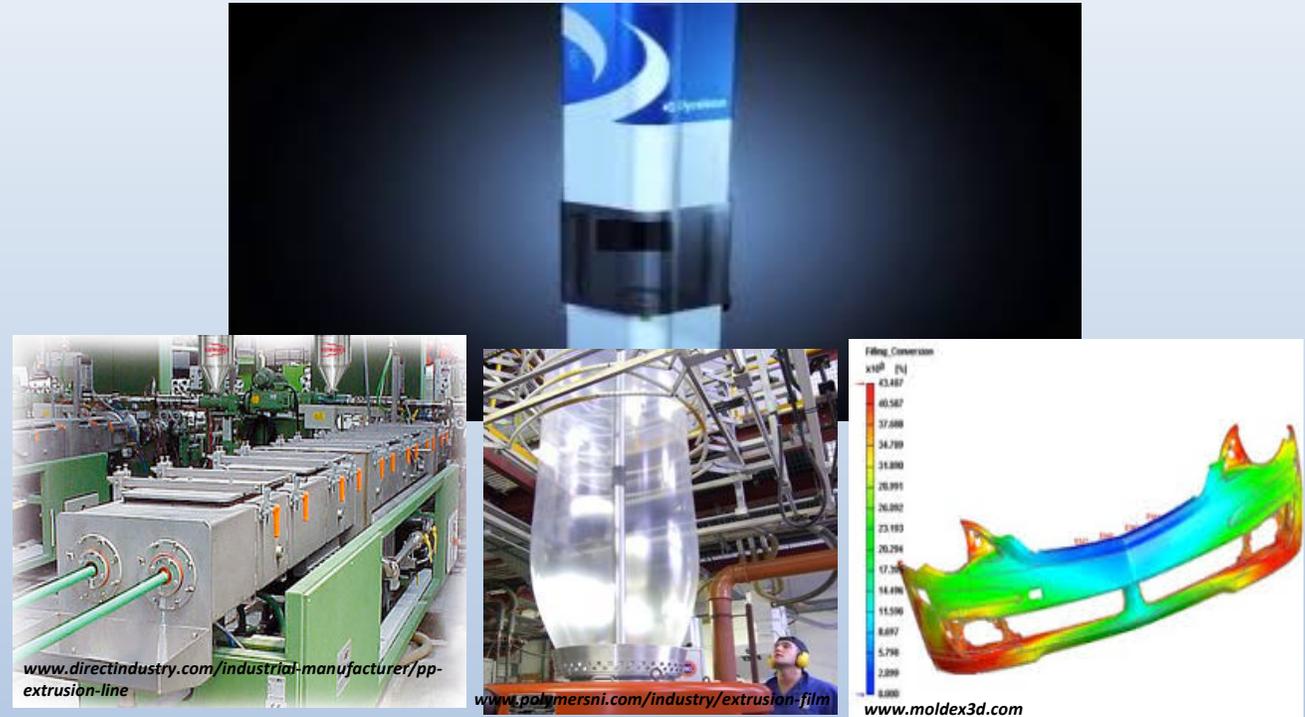


# Introduction

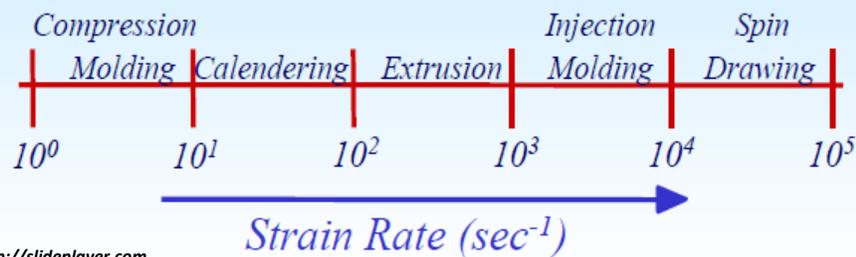


# Why Capillary Rheometer?

- ❖ The most common melt rheometer to analyze flow behavior of polymers under processing condition (shear rate, time, temperature).
- ❖ Duplication of processing parameters for design, simulation, and trouble shooting purposes in a faster way.
- ❖ Predict optimal operating condition based on correlation of rheological data from capillary rheometer to processing parameters.
- ❖ Analyze different materials for various applications and design.



## *SHEAR RATES ENCOUNTERED IN PROCESSING*



<http://slideplayer.com>

## **APPLICATIONS**

- ✓ Polymer viscosity at wide deformation rate range
- ✓ Polymer melt flow behavior
- ✓ Shear thinning behavior
- ✓ Polymer stability over time/temperature
- ✓ Elastic properties (die swell, wall slip)

# Dynisco® LCR 7001

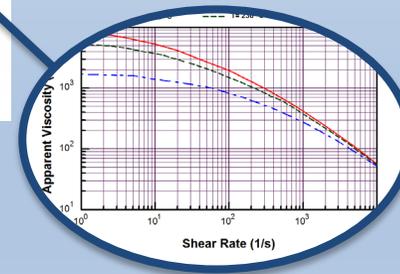
Force measurements  
from Load Cell



Pressure measurement  
from Pressure Transducer



RESULTS:  
Polymer flow curve  
(LabKars Software)



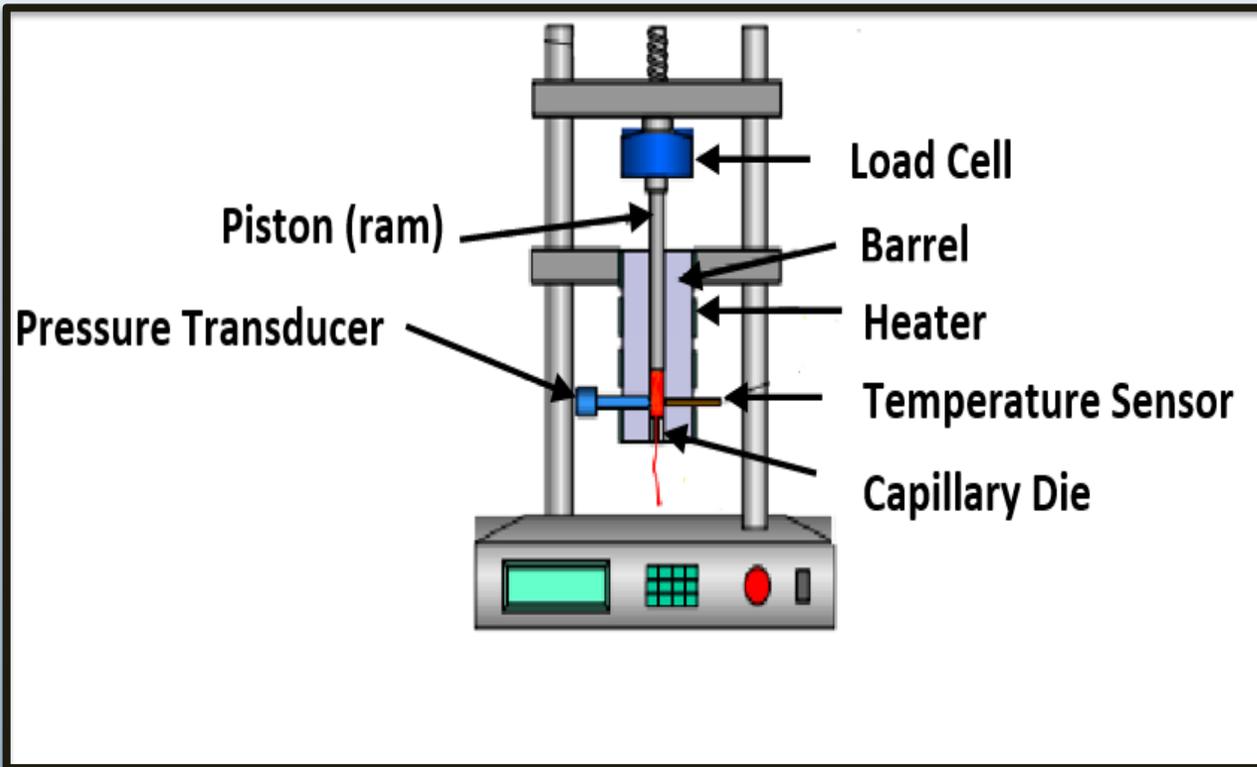
## ❖ MEASURES:

- ✓ Force
- ✓ Pressure
- ✓ Ram rate
- ✓ Time
- ✓ Temperature
- ✓ Expansion of extrudate

## ❖ CALCULATES:

- ✓ Shear stress
- ✓ Shear rate
- ✓ Shear/extensional Viscosity
- ✓ Die swell ratio

# General Specification

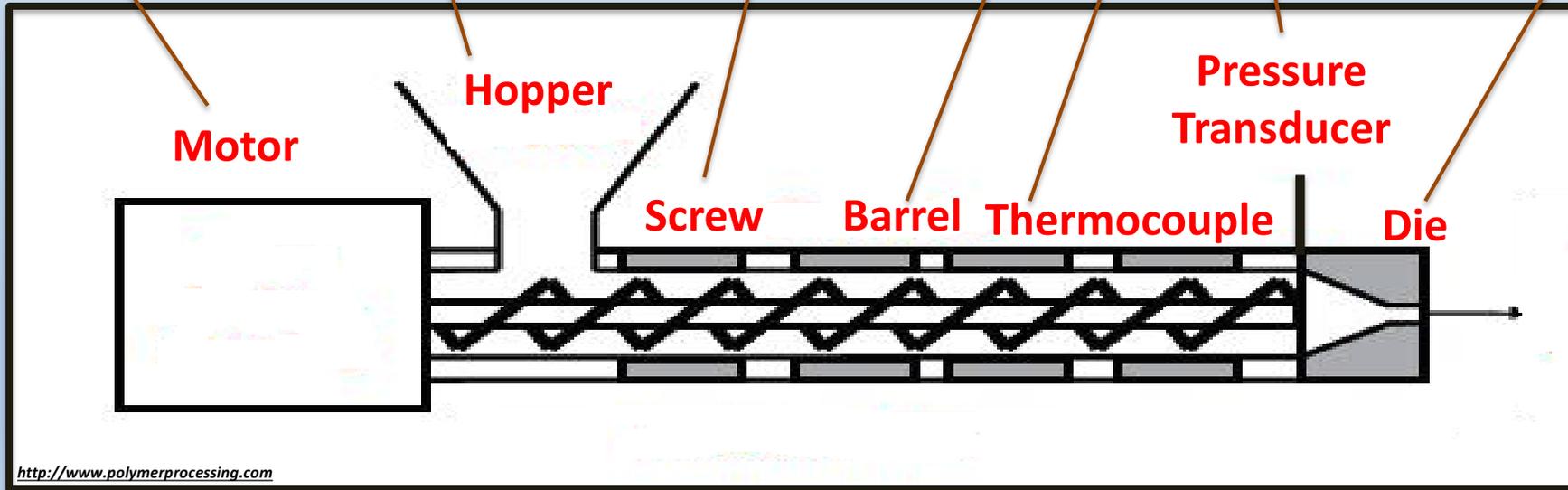
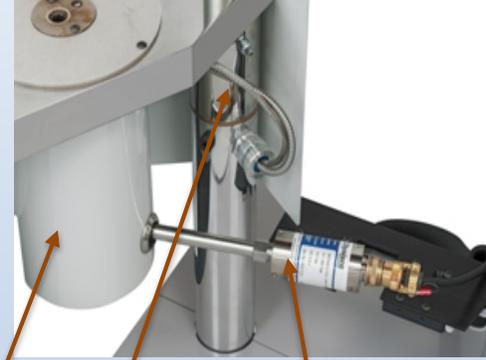
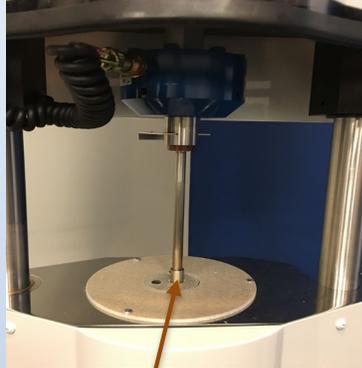
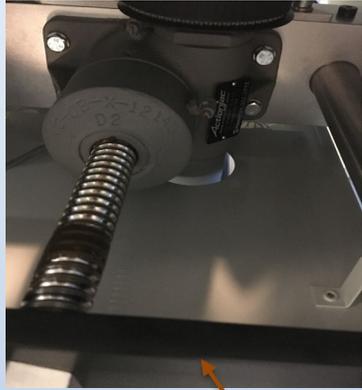


Based on **ASTM-D3835** "Standard Test Method for Determination of Properties of Polymeric Materials by Means of a Capillary Rheometer"

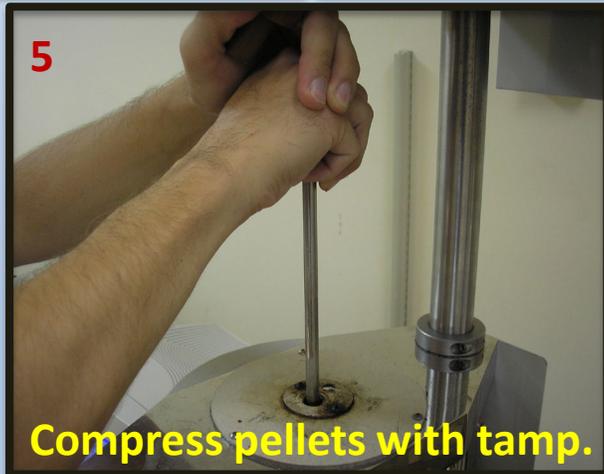
## ❖ LCR7001 SPECIFICATION

- ✓ Temp range: 25-500 °C
- ✓ Shear rate range: 1-100000 1/s
- ✓ Barrel diameter: 9.55 mm
- ✓ Available length: 227 mm
- ✓ Working length: 125 mm
- ✓ Min piston speed: 0.03 mm/min
- ✓ Max piston speed: 650 mm/min
- ✓ Max force measurement from load cell: 10 KN
- ✓ Max pressure measurements: 1400 Bar
- ✓ Accuracy of test-to-test ~1.5-2%
- ✓ Accuracy of rheometer-to-rheometer ~8%

# Extrusion & Capillary Rheometer

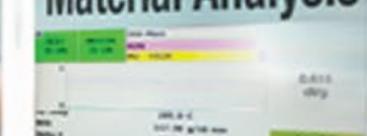
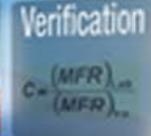


# LCR Preparation Before Running the Test



# LCR Cleaning After the Test

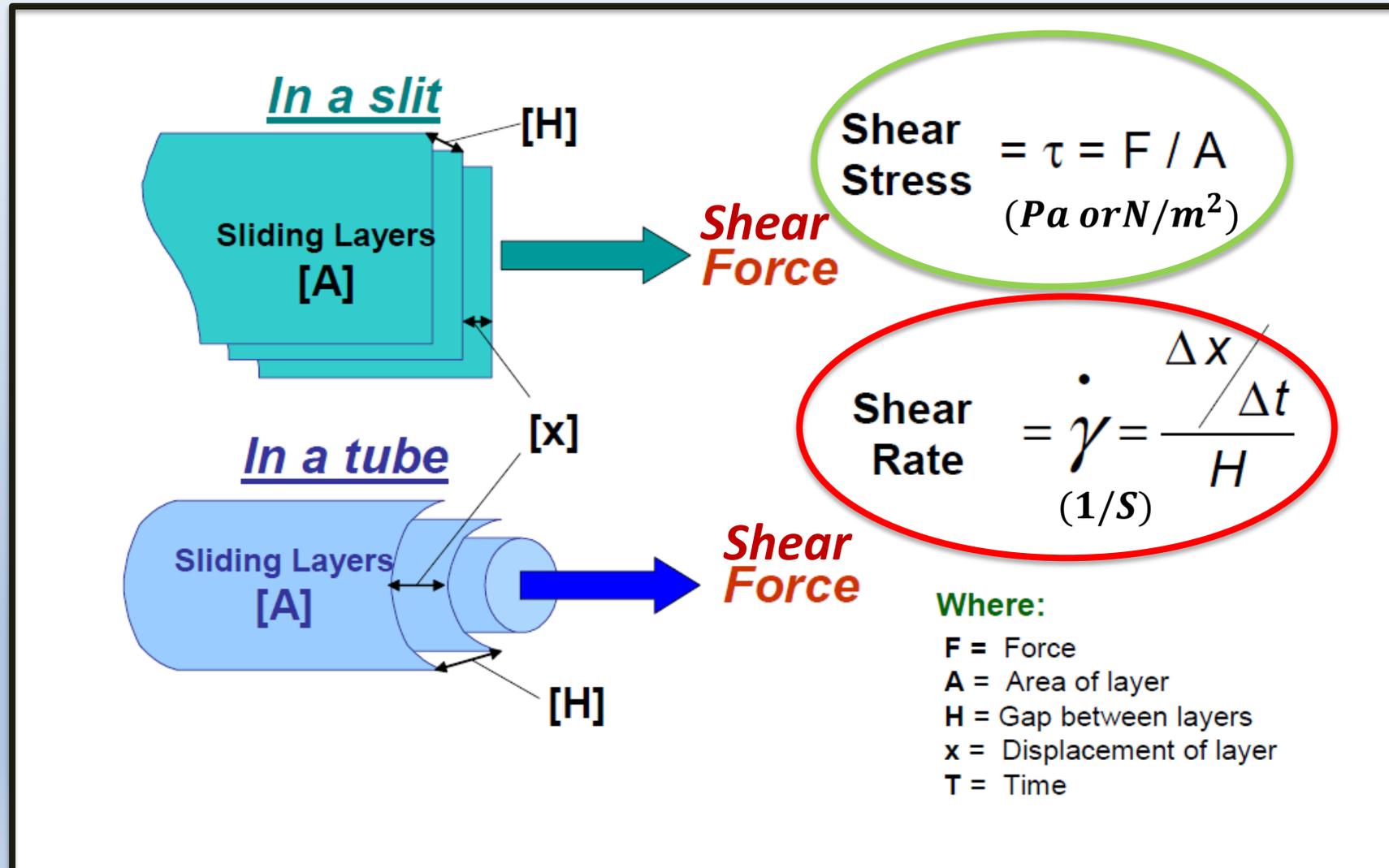




# Shear Sweep Test

## (Polymer Flow Behavior)

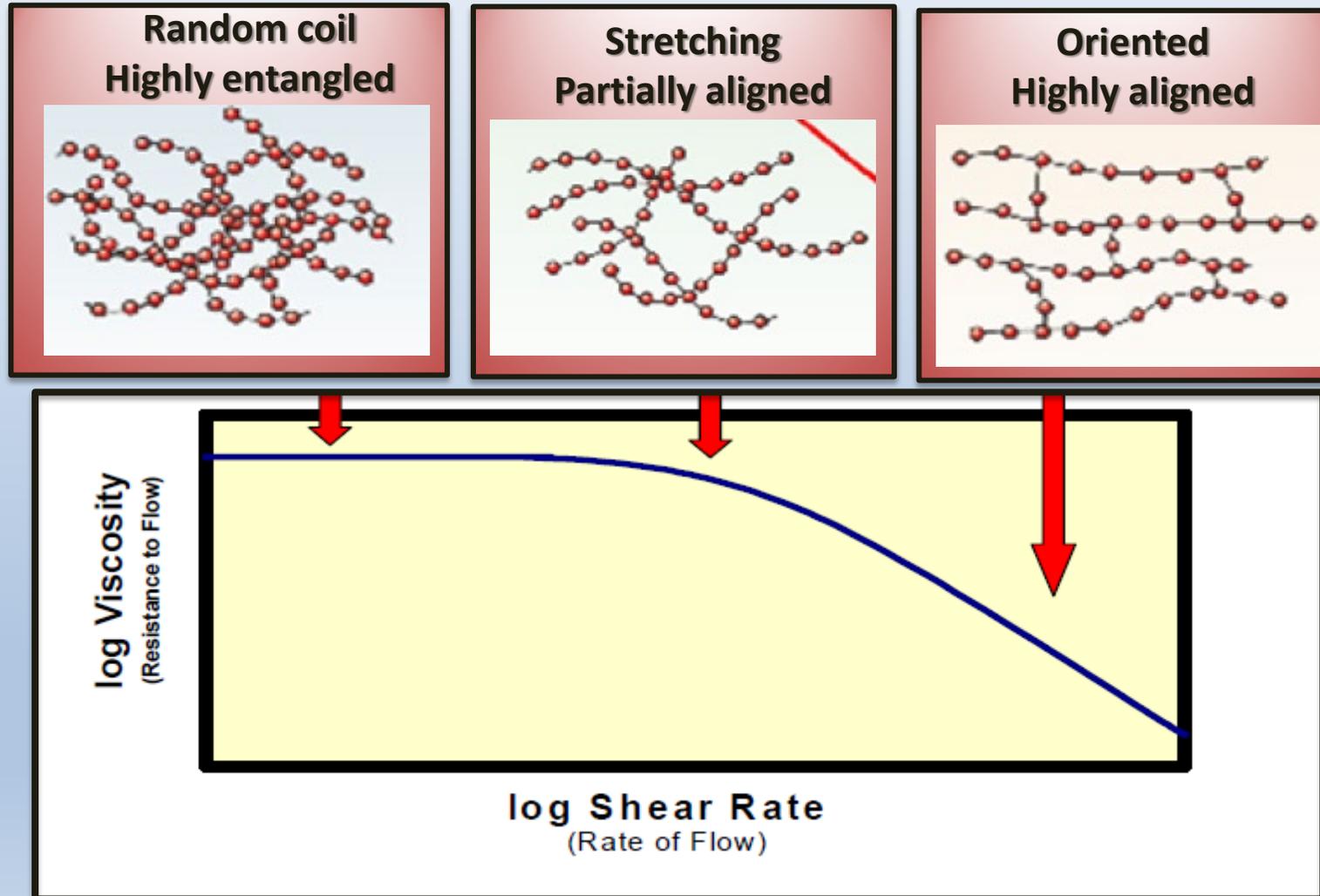
# What is Shear?



# Calculation of Rheological Data in LCR

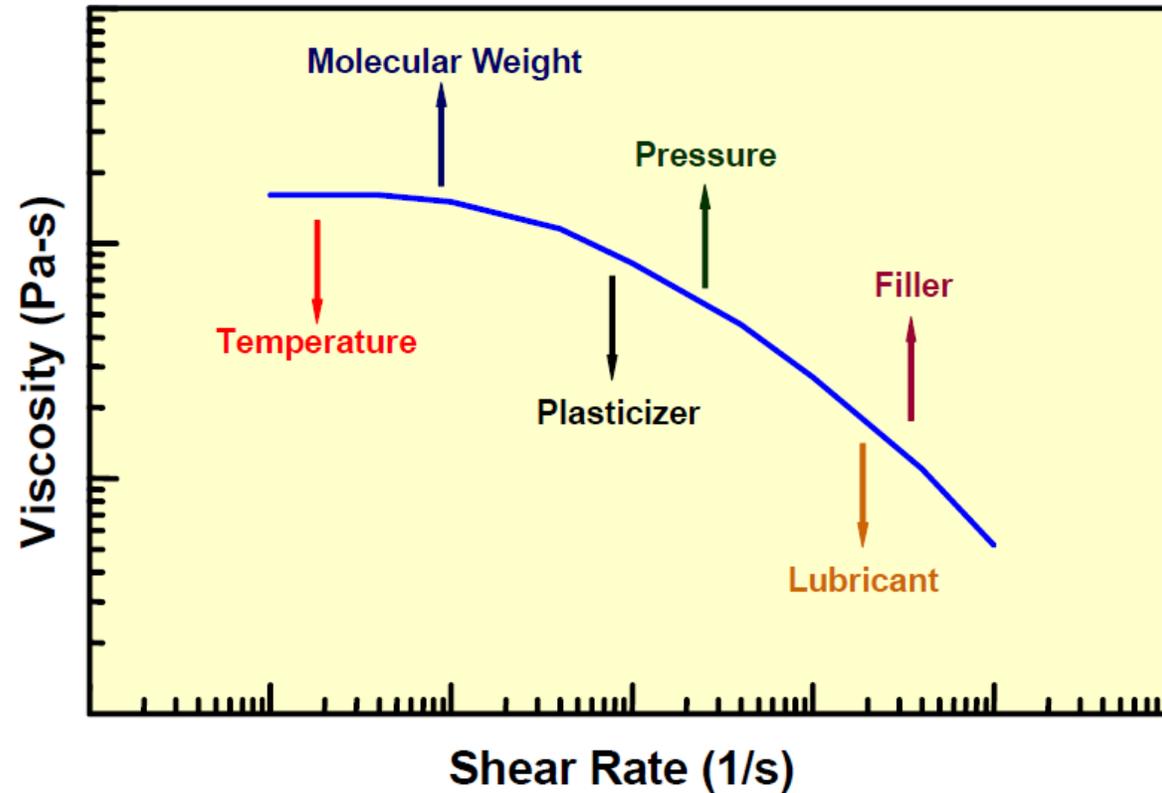
<p><b>Apparent shear rate (based on piston speed)</b></p>	<p>❖ <math>\dot{\gamma}_a = \frac{4Q}{\pi R_c^3}</math></p> <p>❖ <math>Q = S \left( \frac{\pi D_b^2}{4} \right)</math></p> <ul style="list-style-type: none"> <li>➤ <math>\dot{\gamma}_a</math> (1/s): apparent shear rate</li> <li>➤ <math>Q</math> (mm<sup>3</sup>/sec): volumetric flow rate</li> <li>➤ <math>S</math> (mm/min): piston speed</li> <li>➤ <math>D_b</math> (mm): barrel diameter</li> <li>➤ <math>R_c</math> (mm): die radius</li> </ul>
<p><b>Wall shear stress (based on force or driving pressure)</b></p>	<p>❖ <math>\tau_w = \frac{F / \pi D_b^2}{4(L/D)_{die}}</math></p> <p>❖ <math>\tau_w = \frac{P}{4(L/D)_{die}}</math></p> <ul style="list-style-type: none"> <li>➤ <math>\tau_w</math> (Pa): wall shear stress</li> <li>➤ <math>F</math> (N): force from “load cell” on piston</li> <li>➤ <math>D_b</math> (mm): barrel diameter</li> <li>➤ <math>L/D</math>: length to diameter ratio of the die</li> <li>➤ <math>P_d</math> (Pa): driving pressure at the die entrance from “pressure transducer”</li> </ul>
<p><b>Apparent shear viscosity</b></p>	<p>❖ <math>\eta_a = \frac{\tau_w}{\dot{\gamma}_a}</math></p> <ul style="list-style-type: none"> <li>➤ <math>\eta_a</math> (Pa-s): apparent shear viscosity</li> <li>➤ <math>\tau_w</math> (Pa): wall shear stress</li> <li>➤ <math>\dot{\gamma}_a</math> (1/s): apparent shear rate</li> </ul>

# Shear Flow in Viscoelastic Polymer Melts

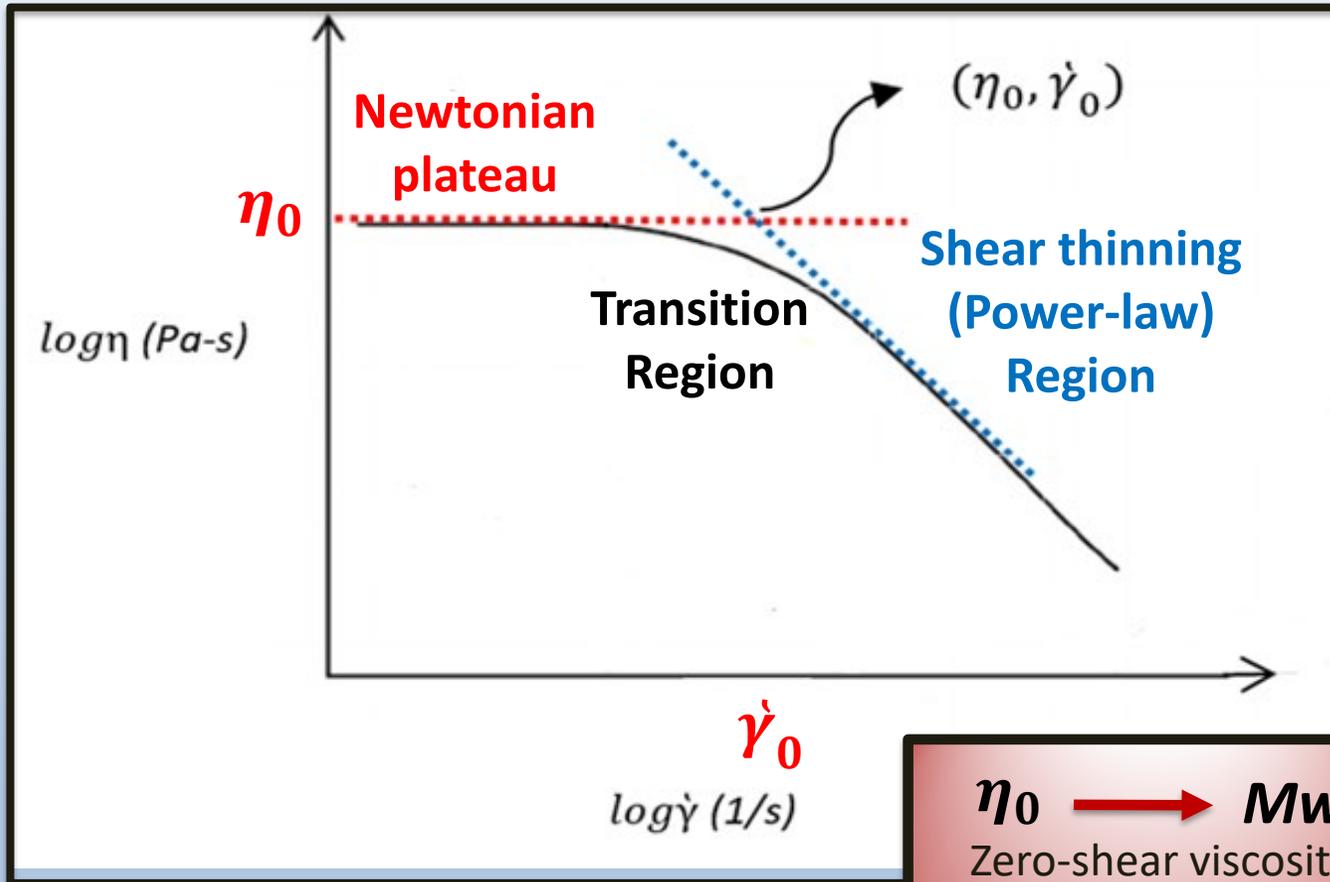


# Effect of Various Factors on Polymer Flow Curve

## How an Increase in Various Factors Affects the Polymer Melt Viscosity Curve

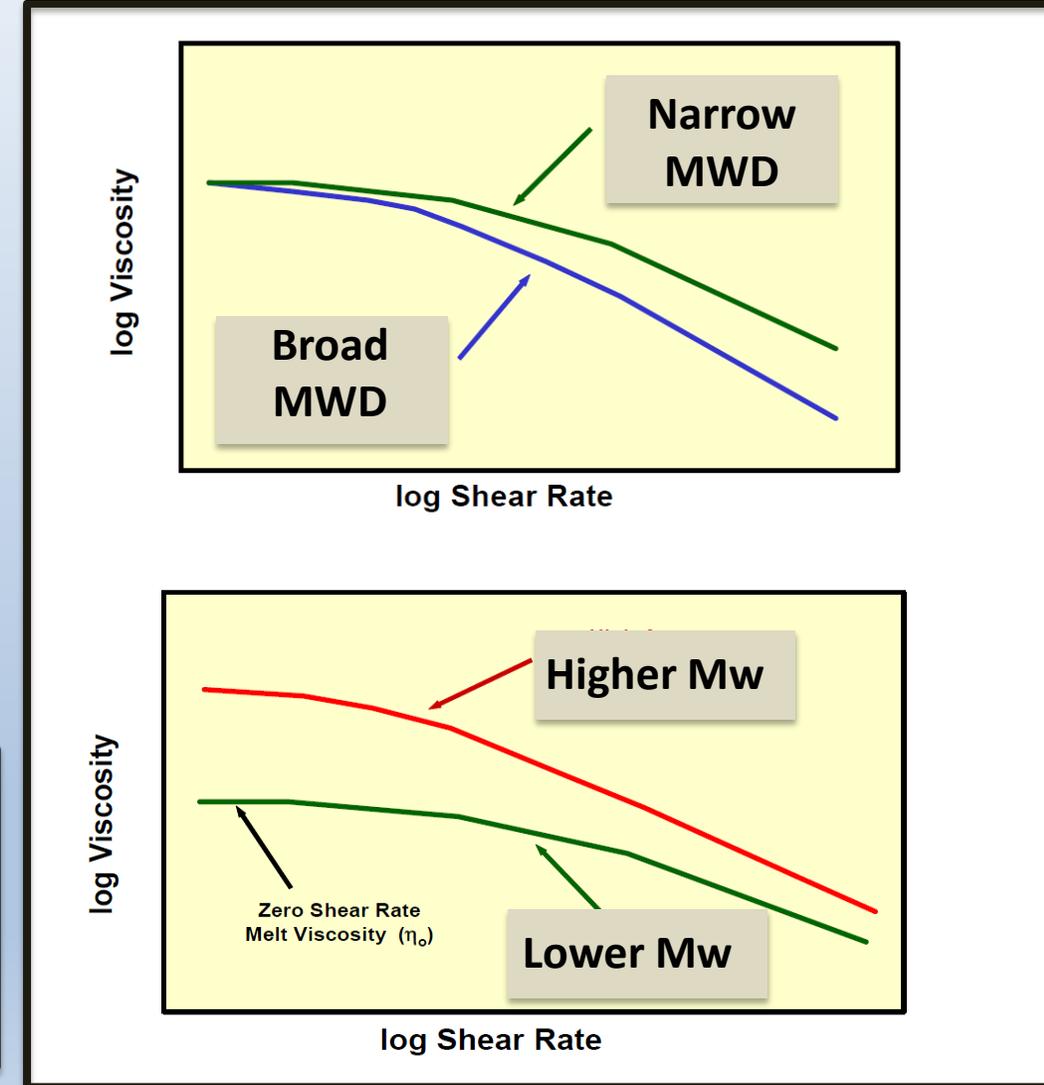


# Flow Curve of Polymer Melts



$\eta_0 \longrightarrow Mw$   
Zero-shear viscosity

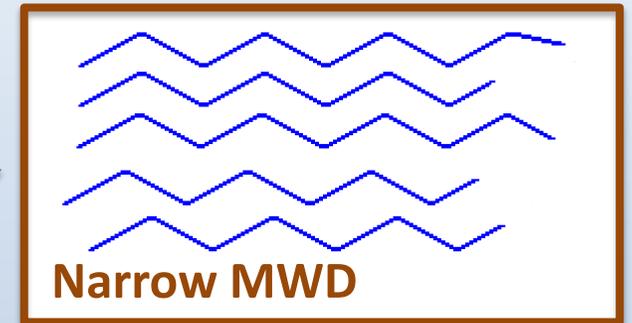
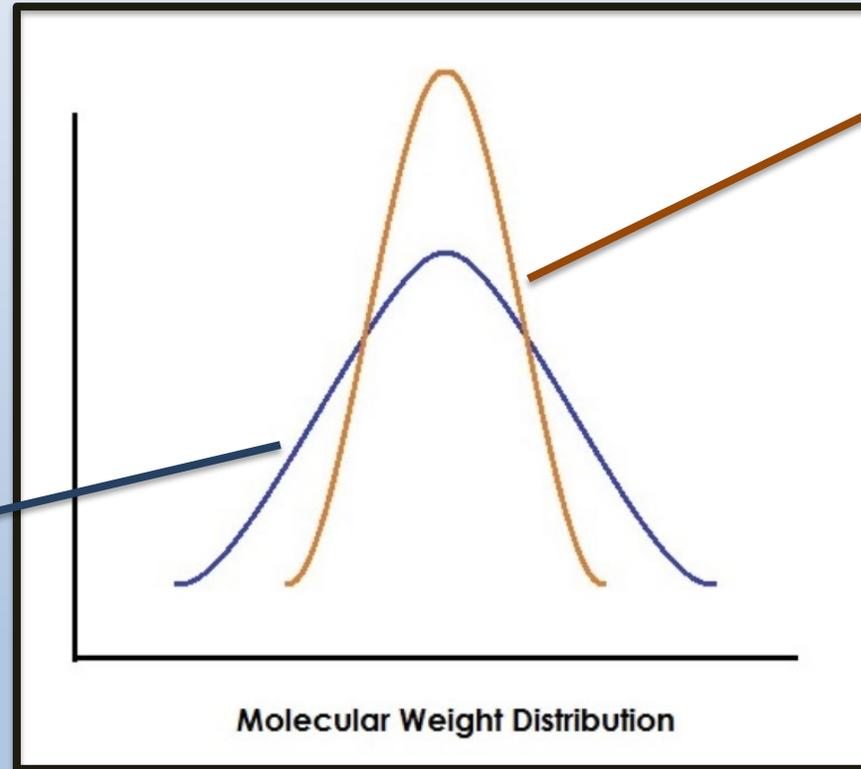
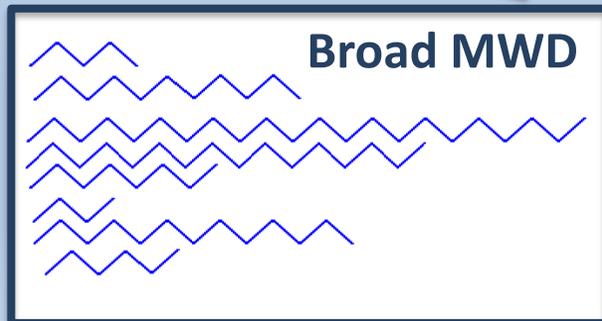
$\dot{\gamma}_0 \longrightarrow MWD$   
Characteristic shear rate



# Molecular Weight Distribution (MWD)

## Polymers with Broader MWD:

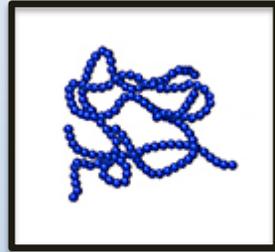
- Better processability (fluidity)
- Less viscous dissipation during their process
- Less energy consumption during their process
- Lower mechanical properties



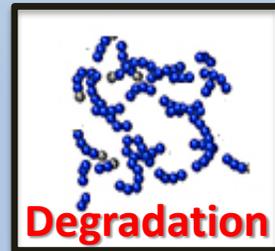
# Analyzing Polymer Degradation from Flow Curve

Flow curve of plastic samples before process and after process at various screw speeds in an extrusion

Higher  $\eta_0$  and  $M_w$



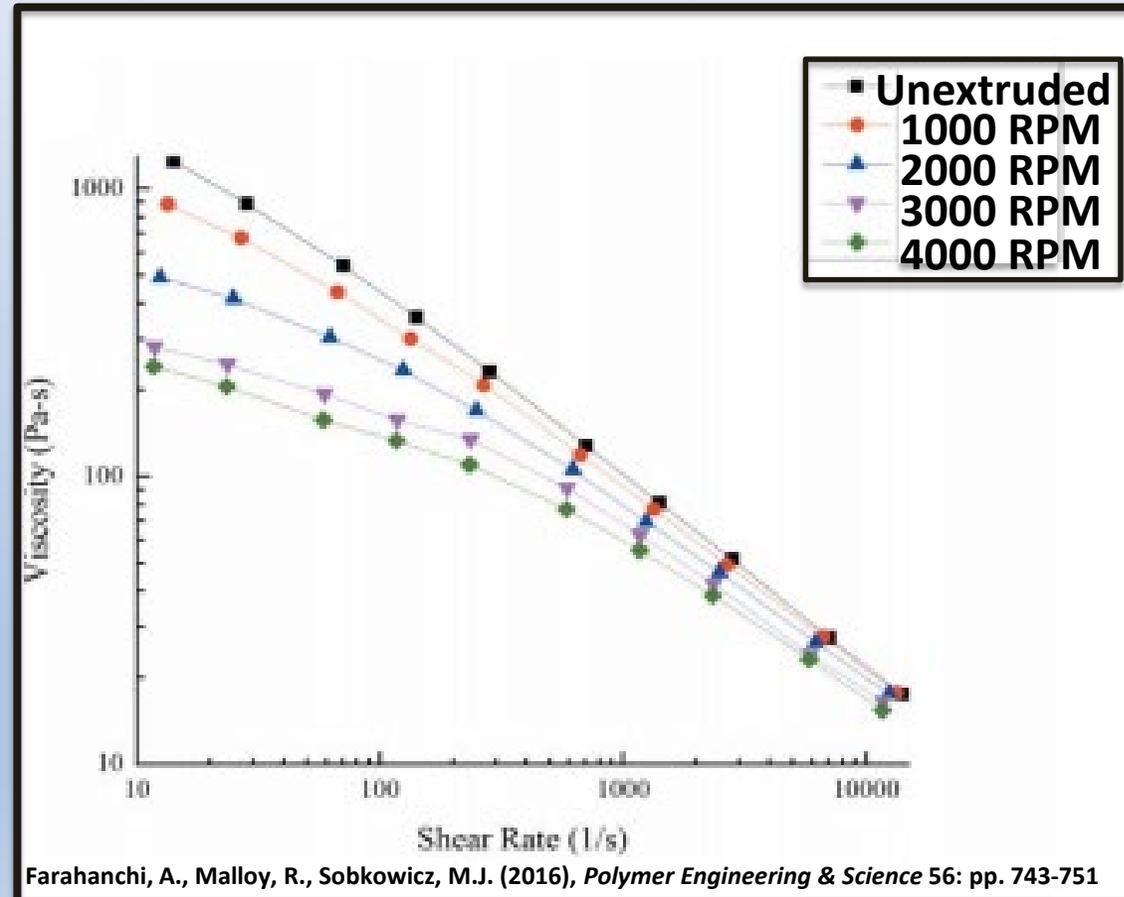
Lower  $\eta_0$  and  $M_w$



## Extrusion Condition

Heat

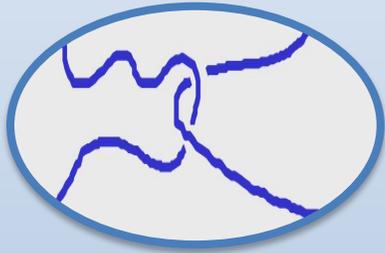
- Barrel temp
- Mechanical shear
- Screw speed
- Residence time
- Flow rate



Farahanchi, A., Malloy, R., Sobkowicz, M.J. (2016), *Polymer Engineering & Science* 56: pp. 743-751

# Mw Dependence of Zero-Shear Viscosity

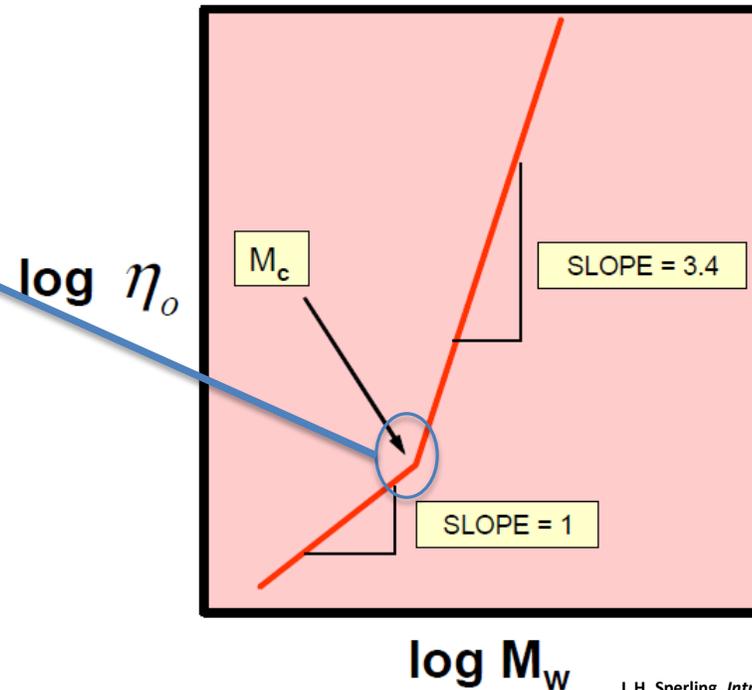
*Critical Molecular wt. ( $M_c$ )*  
molecular entanglements occur



Polymers with higher Mw:

- ✓ Higher intermolecular entanglement
- ✓ Higher strength
- ✓ Higher chemical resistance

## Relationship of the Molecular Weight to Melt Viscosity



Fox-Flory Equation

$$\eta_0 = K_2 (M_w)^{3.4}$$

Where:

$\eta_0$  = "Zero shear rate"  
melt viscosity.

$K_2$  = Constant

$M_w$  = Wt. avg. molecular wt.

$M_c$  = "Critical" molecular wt.

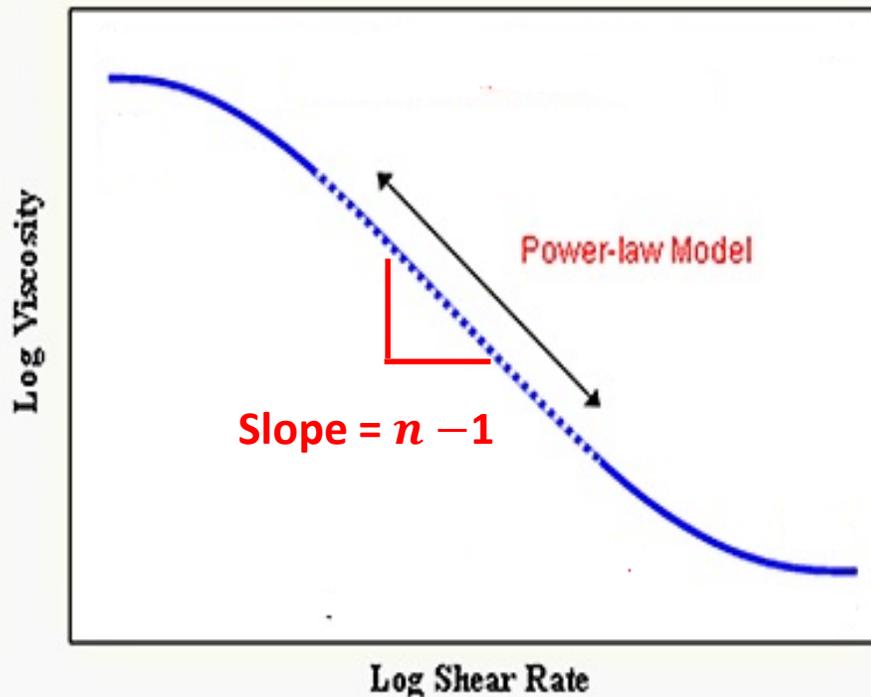
L.H. Sperling, *Introduction to Physical Polymer Science*, John Wiley & Sons, 4<sup>th</sup> Edition.

# Quantitative Relationships for the Dependence of Viscosity upon Shear Rate

## Power-law Model

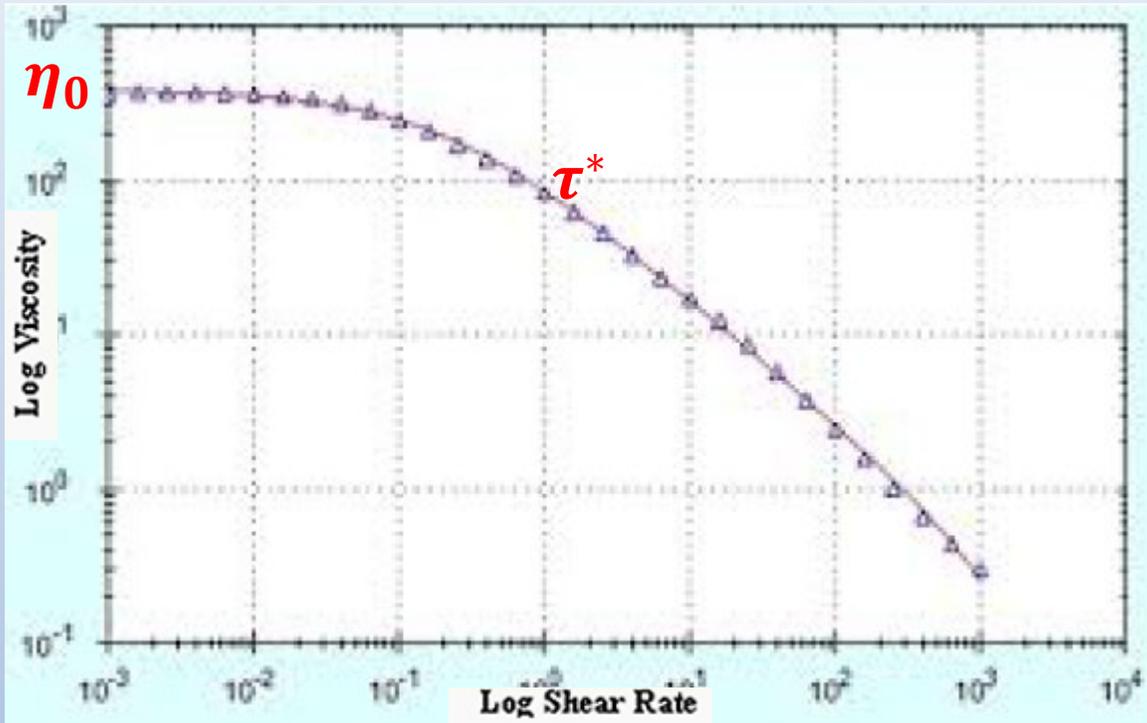
$$\eta(\dot{\gamma}) = k\dot{\gamma}^{n-1}$$

- $k$  (Pa-s): Consistency
- $n$ : Power-law index



- ❖ “Only” fits the shear-thinning (power-law) portion of the curve
- ❖ Shear-thinning exponents dependent on intermolecular forces.
- ❖  $n$  ranges from 0.2-0.9 depending upon the type of polymer.
- ❖  $n$  equals to 1 for Newtonian materials.
- ❖  $n$  represents the processability (shear-thinning intensity).
- ❖ Polymers with lower  $n$  are more sensitive to the shear rate.
- ❖  $n$  decrease with broader MWD.
- ❖  $k$  has temperature dependency and controlled by Mw.

# Quantitative Relationships for the Dependence of Viscosity upon Shear Rate



## Modified Cross Model

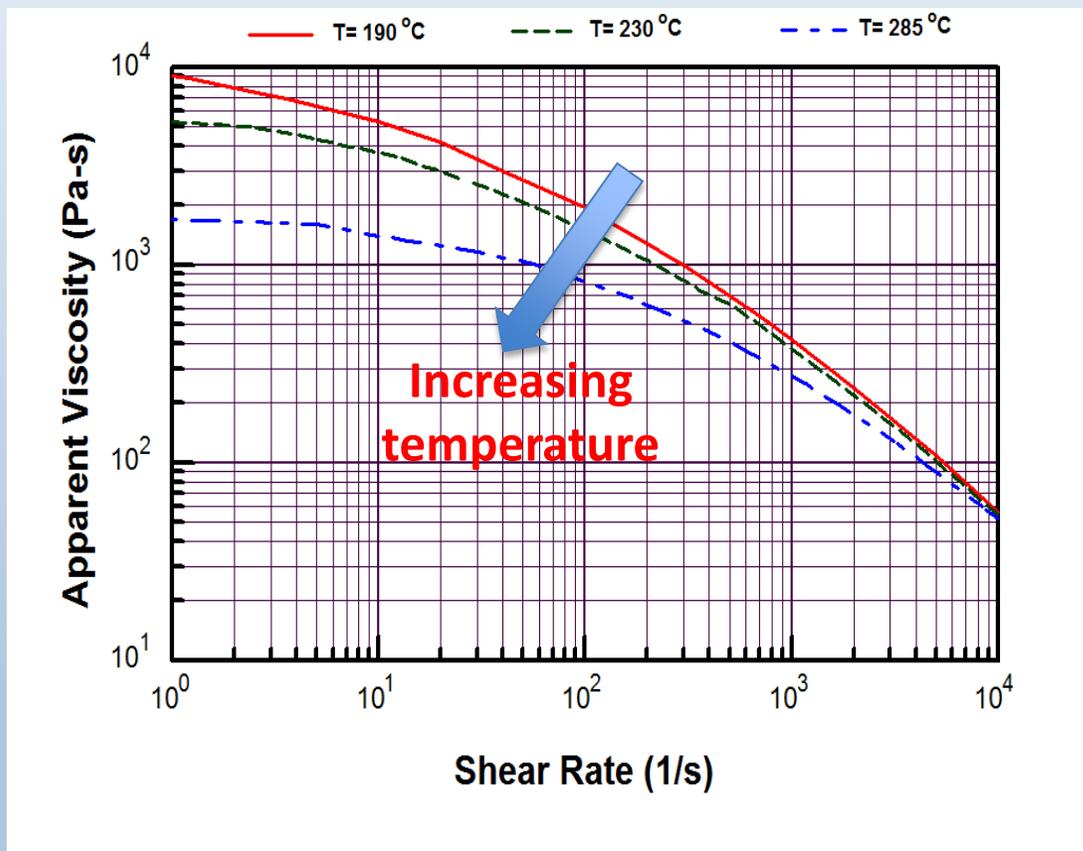
$$\eta(\dot{\gamma}) = \frac{\eta_0}{1 + \left(\frac{\eta_0 \dot{\gamma}}{\tau^*}\right)^{1-n}}$$

- $\eta_0$  (Pa-s): Zero-shear viscosity
- $\tau^*$  (Pa): Critical shear stress
- $n$ : Power-law index

- ❖ Combines the power-law and Newtonian regions.
- ❖ Also fits the low shear Newtonian plateau.
- ❖  $\eta_0$  is controlled by molecular weight.
- ❖  $\tau^*$  is stress at the beak in curve and controlled by MWD.
- ❖ Broader MWD (by blending or branching) cause earlier  $\tau^*$ .

# Viscosity-Temperature Dependence

## Window into the process



❖ Williams-Landel-Ferry (WLF) model: ( $T_g < T < T_g + 100$ )

$$\log(a_T) = \frac{\eta_0(T)}{\eta_0(T_{ref})} = \left[ \frac{-C_1(T - T_g)}{C_2 + T - T_g} \right]$$

$$C_1 = 17.44$$

$$C_2 = 51.6 \text{ K}$$

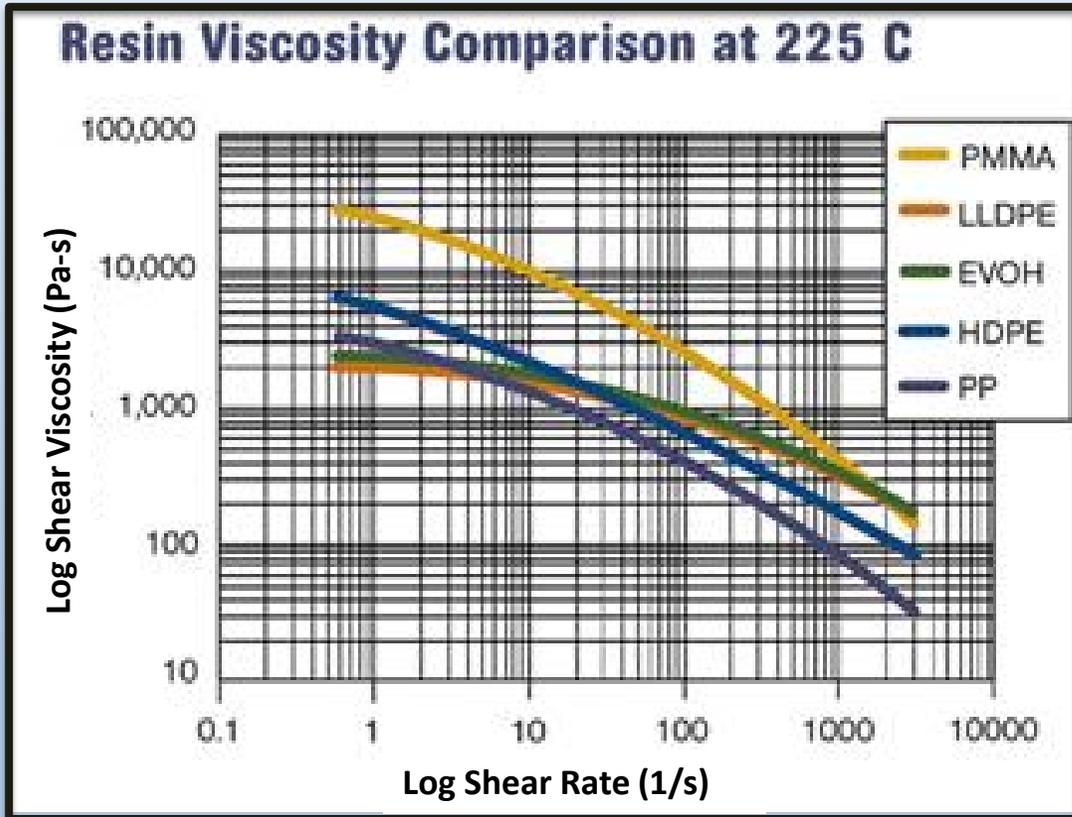
❖ Arrhenius model: ( $T > T_g + 100$ )

$$a_T = \frac{\eta_0(T)}{\eta_0(T_{ref})} = \exp\left[\frac{E_a}{R} \left(\frac{1}{T} - \frac{1}{T_{ref}}\right)\right]$$

$E_a$ : Activation Energy

$R$ : Universal gas constant =  $8.314 \times 10^{-3} \text{ kJ/mol.K}$

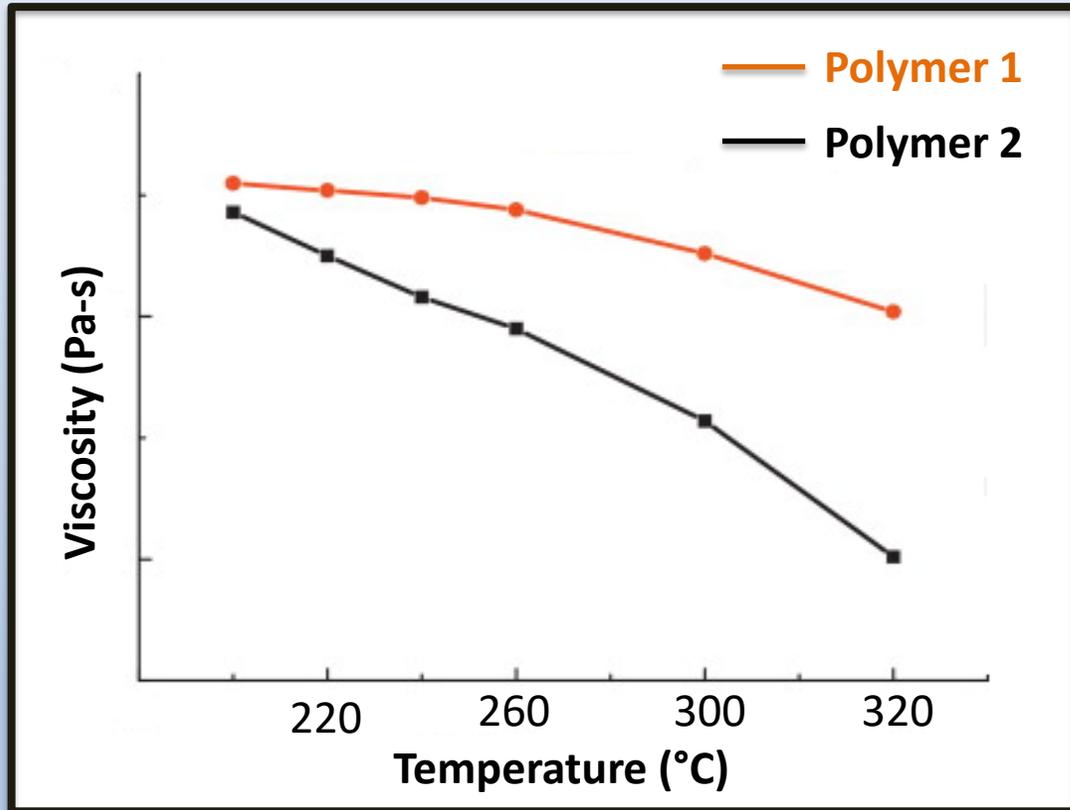
# A Window into Your Process!



<https://www.ptonline.com/columns/how-to-spec-a-flat-die>

- At shear rate 100-1000 1/s (common at normal RPM in extrusion), the processing of which polymer cause higher torque and head pressure, and viscous heating in the extrusion?
- Which polymer has higher shear-thinning behavior (easier process-ability)?
- With increasing screw speed which polymer will have the highest flow rate?
- Which polymer has the highest molecular weight?
- Which polymer had the Broader MWD?
- Which polymer might have linear might have long chain-branching and which one might have linear structure?

# A Window into Your Process!



- Which polymer might face higher thermal degradation with increasing temperature?
- Which polymer has wider processing temperature?

# Shear-Sweep Test Setup in LabKars

The screenshot shows the LabKars software interface for setting up a Shear-Sweep test. The main window is titled 'Setup' and contains a table of data points for 'Data Point Setup # 312'. The table has columns for Setup #, Program Name, Start Pos., Temperature, Melt Time, Sensor1 ID, and Die. The first row is highlighted in blue.

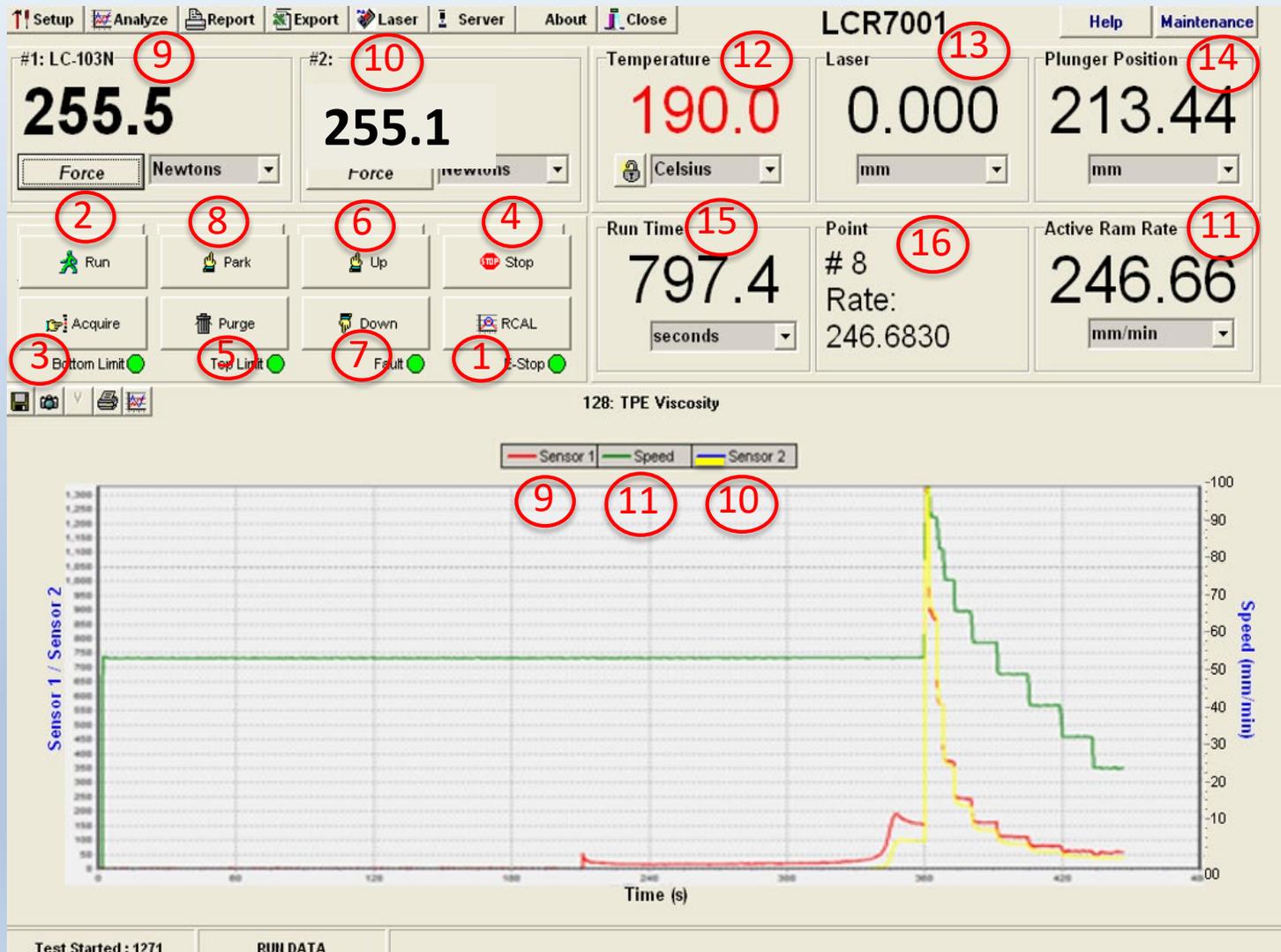
Setup #	Program Name	Start Pos.	Temperature	Melt Time	Sensor1 ID	Die
312	Shear Rate Sweep	100	190	300	LC-502N	CX394-30
313	PE Sweep	100	190	300	LC-502N	CX394-30
314	PE Stability	100	190	300	LC-502N	CX394-30
315	PE Stability II	100	190	300	LC-502N	CX394-30
316	PE Short	100	190	300	LC-502N	CX394-30
317	PE Long	100	190	300	LC-502N	CX394-30
318	PE Slip Small	100	190	300	LC-502N	CX394-30
319	PE Slip Large	100	190	300	LC-502N	CX394-30
320	PP Sweep	100	190	300	LC-502N	CX394-30
321	PP Stability	100	190	300	LC-502N	CX394-30

Below the table, there are control options for 'Control Mode' (Rate selected) and 'Test Type' (Steady State selected). A 'Sweep Generation' dialog is open, showing 'Point' and 'Speed Control' columns. The 'Start' point is 1 and the 'End' point is 10. The 'Value in Speed Control' checkbox is checked. The 'Generate Method' is set to 'Logarithmic'. The 'Auto Generate Points' button is visible.

At the bottom, there are input fields for 'Minimum Speed' (0.03) and 'Maximum Speed' (650). A 'Send' button is located at the bottom right.

1. Add/delete Data Point Setup
2. Program Name
3. Start Position (mm): 89-100 mm
4. Temperature (°C): barrel temperature set point
5. Melt time (sec): 180-360 sec
6. Sensor1 ID: LC-103N
7. Die: choose entrance angle, D and L/D from list
8. Minimum/Maximum Speed (mm/min):  
Min at 0.03 and Max at 650 mm/min
9. Data Acquisition mode:  
Steady state, Position, Time Delay, Manual
10. Speed Control range (mm/min)
11. Shear Rate range (1/s)
12. Send: sending test setup to rheometer

# LabKars Software (Control Screen)



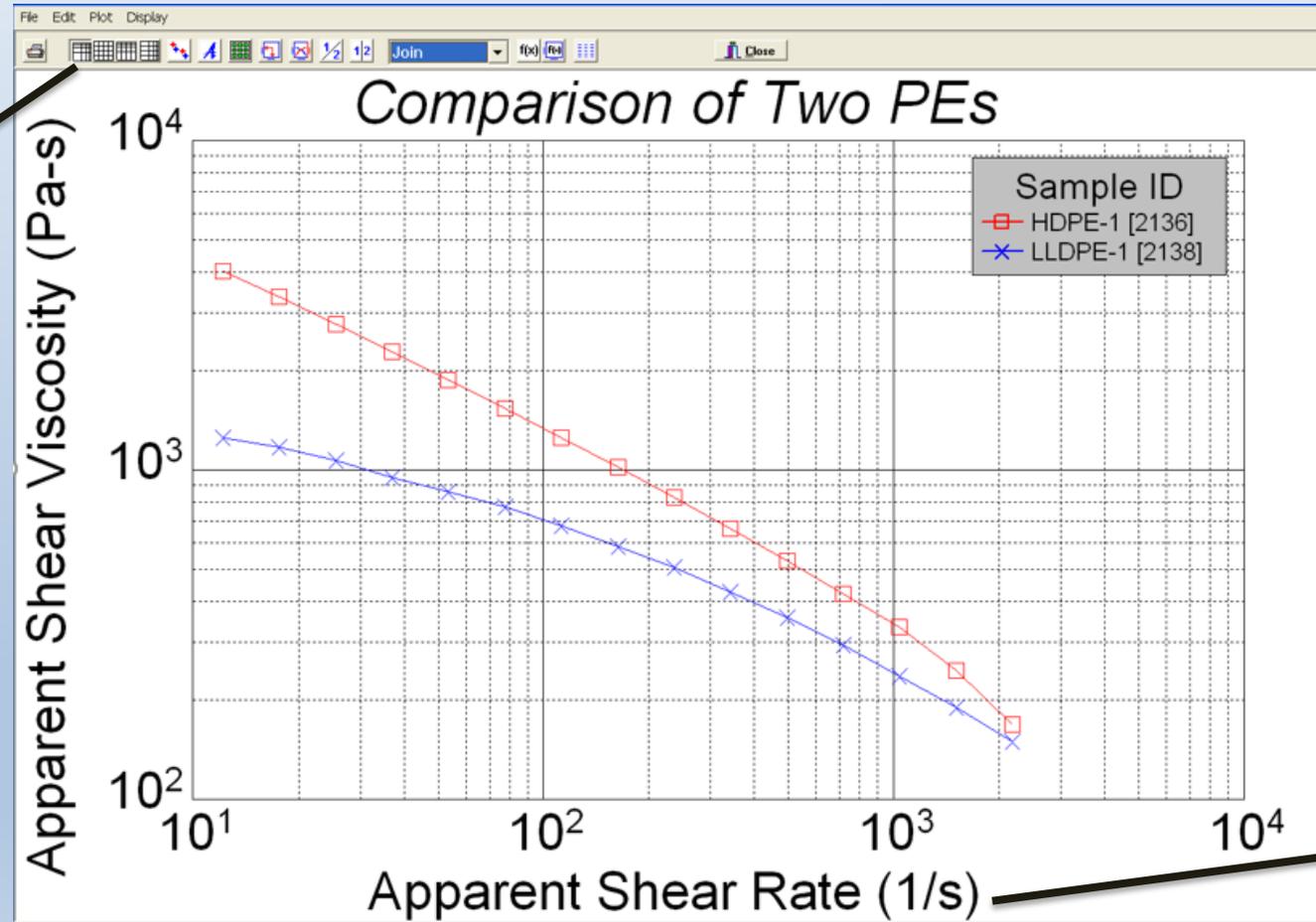
## Real-time data graph during the test

- RCAL:** balance transducers!
- Run:** run the test!
- Acquire:** collect data!
- Stop:** stop the test!
- Purge:** purge all the material in barrel!
- Up:** move plunger upward!
- Down:** move plunger downward!
- Park:** go to park position (25mm)!
- Sensor #1 (N):** force on load cell
- Sensor #2 (N):** force on pressure transducer
- Active Ram Rate (mm/min):** piston speed
- Temperature (°C):** actual barrel temperature
- Laser (mm):** die swell detection
- Plunger position (mm)**
- Run time (sec)**
- Collected point:** at each shear rate

# Data Analysis

## Plot of log apparent viscosity versus apparent shear rate

Click to make logarithmic scale

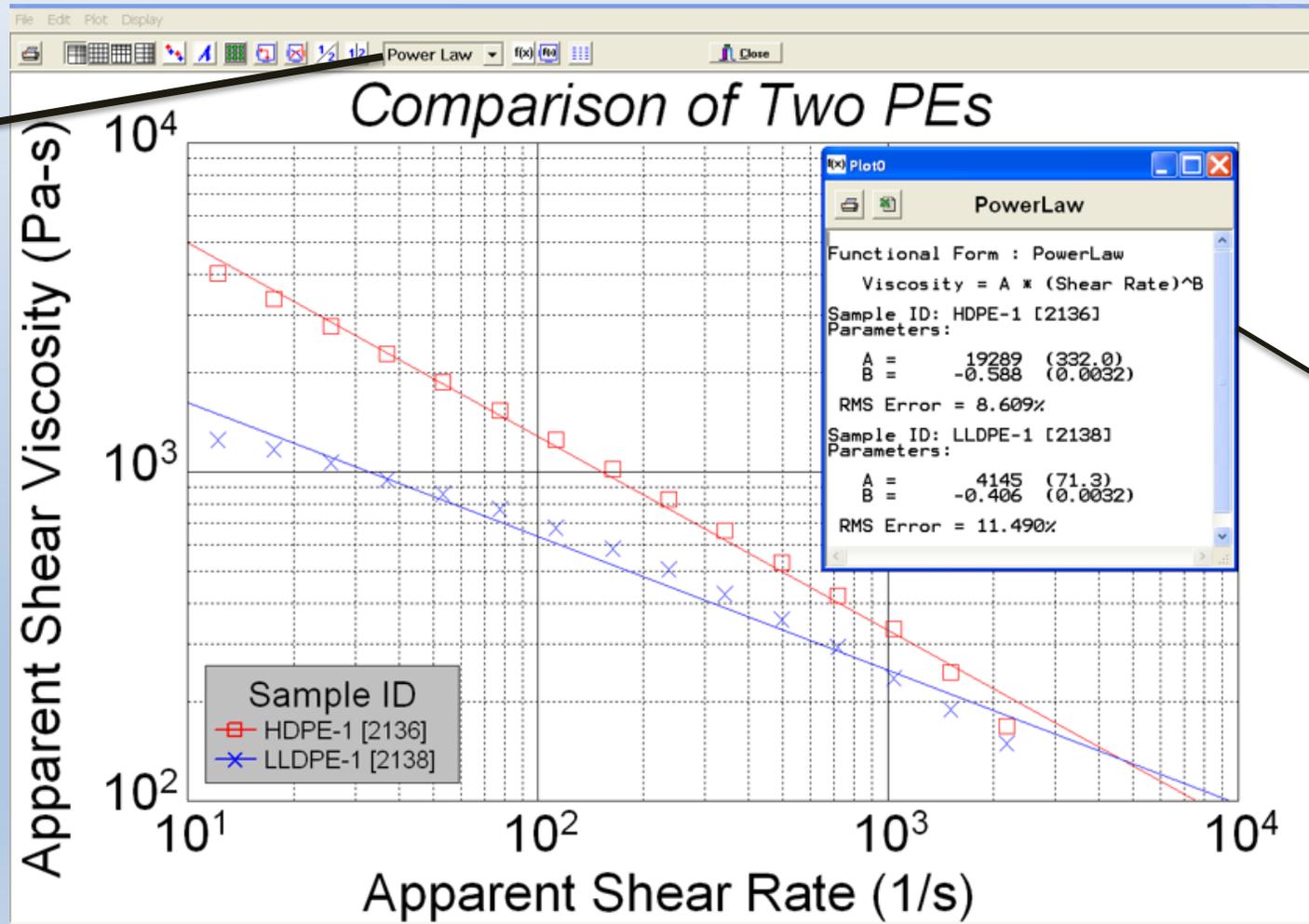


Right Click to change the axis

# Data Analysis

## Power-law model analysis

Choose  
"Power Law"

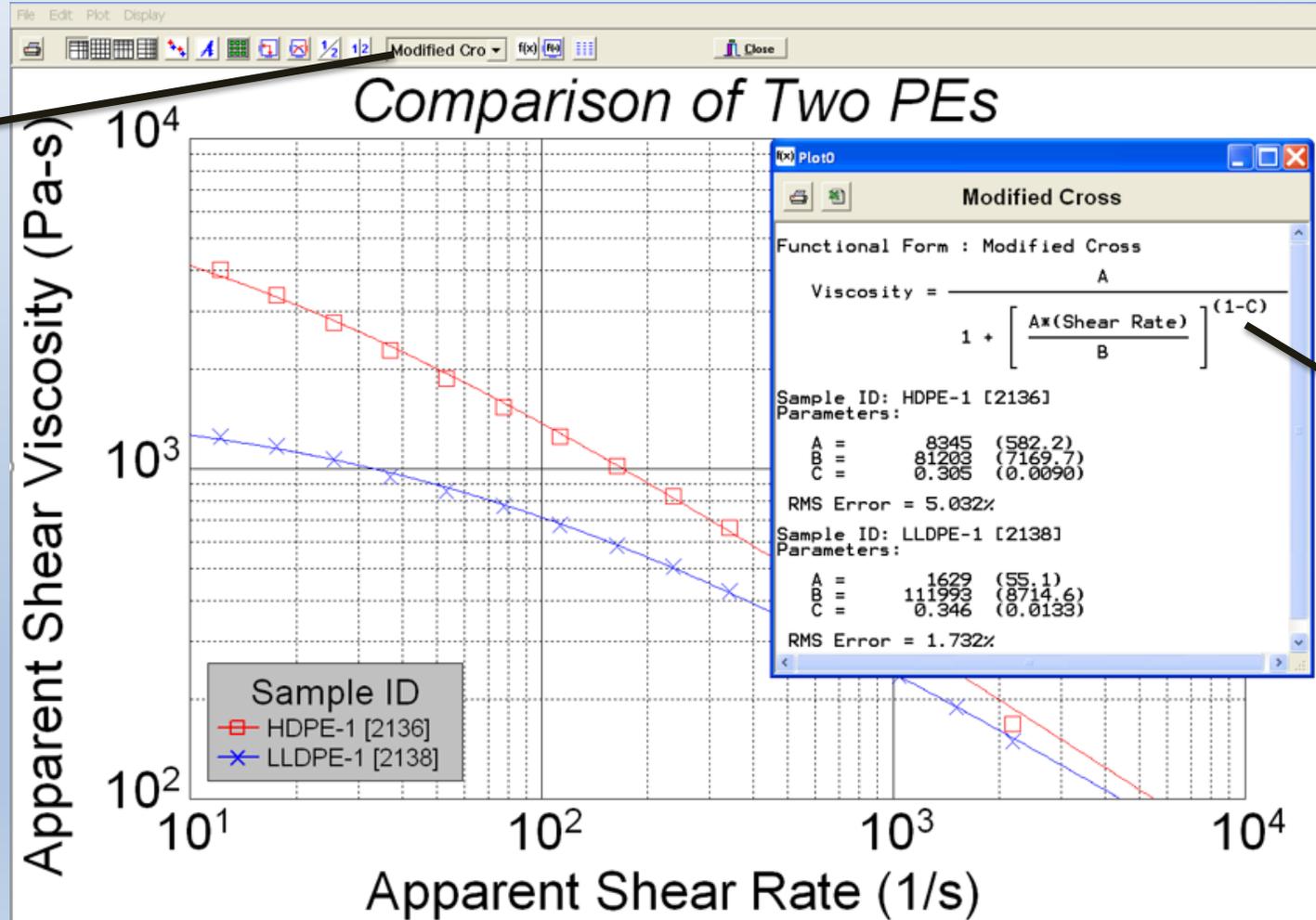


Power law  
fitting data

# Data Analysis

## Modified cross model analysis

Choose  
"Modified Cross"



Modified cross  
fitting data

# Raw Data in LabKars

The screenshot shows the 'Dynisco Polymer Test - Analyze' software interface. At the top, there is a menu bar (File, Edit, Plot) and a toolbar with buttons for Print, Plot, Refresh, Copy, and Close. The 'Plot' button is circled in red. Below the toolbar, there are tabs for 'Database / filters', 'Single Run / Modify', 'Interpolate', and 'Plot Table'. The 'Single Run / Modify' tab is active. The main area contains various test parameters such as Charge #, Points, Operator, Material, Machine, Date, Die, Sample ID, Lot #, Sensor 1, Sensor 2, Melt Time, RCal, Temperature, Melt Pause, Start Position, and Program Name. A 'Select Report Type' section has radio buttons for 'Sensor 1', 'Sensor 2', and 'Sensor 1 & 2'. A 'Printer Format' section has radio buttons for 'Portrait' and 'Landscape'. Below the parameters is a table with columns: Point, Sensor1 (N), Pos (mm), Ram (mm/min), Time (sec), Stress (Pa), Rate (1/s), Visc. (Pa-s), Real Temp (C), and Delay Time. The table contains 6 rows of data. At the bottom, there is a summary table with columns: Force, Position, Ram rate, Time, Stress, Rate, and Viscosity. The summary table includes rows for Average, Max, Min, Count, Mean, and St. Dev. The Windows taskbar at the bottom shows the start button and several open applications.

Point	Sensor1 (N)	Pos (mm)	Ram (mm/min)	Time (sec)	Stress (Pa)	Rate (1/s)	Visc. (Pa-s)	Real Temp (C)	Delay Time
1	198	105	1.13	631.89	46139	1.72	28818.6	210	0
2	199	110	0.98	931.13	46281	1.49	31018.3	210	0
3	206	115	1.20	1229.09	47838	1.83	26183.8	210	0
4	930	140	61.27	1260.60	216402	93.29	2319.8	210	0
5	958	165	72.97	1282.65	222771	111.10	2005.1	209.8	0
6	962	190	80.80	1302.18	223761	123.01	1819.0	209.9	0

	Force	Position	Ram rate	Time	Stress	Rate	Viscosity
Average:	575.4	137.5	36.4	1106.3	133865	55.4	15027.4
Max:	961.8	190.0	80.8	1302.2	223761	123.0	31018.3
Min:	198.3	105.0	1.0	631.9	46139	1.5	1819.0
Count:	6	6	6	6	6	6	6
Mean:	575.377	137.508	36.392	1106.253	133865.300	55.406	15027.430
St. Dev:	410.315	34.177	39.153	269.850	95462.460	59.610	14315.950

Select "Single Run/Modify" to see the raw data

Select the type of sensor

- Sensor 1: Load cell
- Sensor 2: Pressure transducer

Max, min, average, mean, and standard deviation information of all parameters

Raw data

# Export Raw Data in Excel

Capillary Rheometer Control Center

LCR 7001

#1: LC-103N Diff. #1-#2 9.9 #2: PT-142BAR

Temperature 200.0

Plunger Position 25.34

1.8 -1.1

Export to Excel

Switch Database Database Path: d:\PROGRA~1\LABKAR~2\Database

Charge	DateTime	Sample ID	Operator	Material	Lot	Die	Die ID
1261	09/06/2007 01:17 pm	LDPE	MC	HDPE	Low Stress First with intermediate	CX394-20	CX3
1262	09/06/2007 01:51 pm	2.5 N	MC	HDPE	Low Stress First with intermediate	CX394-20	CX3
1263	09/06/2007 03:52 pm	2.5 N	MC	HDPE	Low Stress First with intermediate	CX394-20	CX3
1264	09/07/2007 09:17 am	2.5 N	MC	HDPE	787 Die	CZ787-15	CZ7
1265	09/07/2007 03:48 pm	2.5 N	MC	HDPE	787 Die	CZ787-15	CZ7
1266	09/07/2007 04:15 pm	2.7 N	MC	HDPE	787 Die	CZ787-15	CZ7
1267	09/10/2007 08:59 am	2.7 N	MC	HDPE	9-10-07	CZ787-15	CZ7
1268	09/10/2007 09:31 am	2.7 N	MC	HDPE	9-10-07	CZ787-15	CZ7
1269	09/10/2007 10:04 am	2.5 N	MC	HDPE	9-10-07	CZ787-15	CZ7
1270	09/10/2007 10:37 am	2.5 N	MC	HDPE	9-10-07	CZ787-15	CZ7

Starting Row #: 10 Export To: Single File Multiple Files Charge #: 1270

Status READY

Time (s)

Select "Export"

Select "Single File" to export the data in Excel

Choose your data set

Raw data in Excel sheet



*From lab to production,  
providing a window into the process*



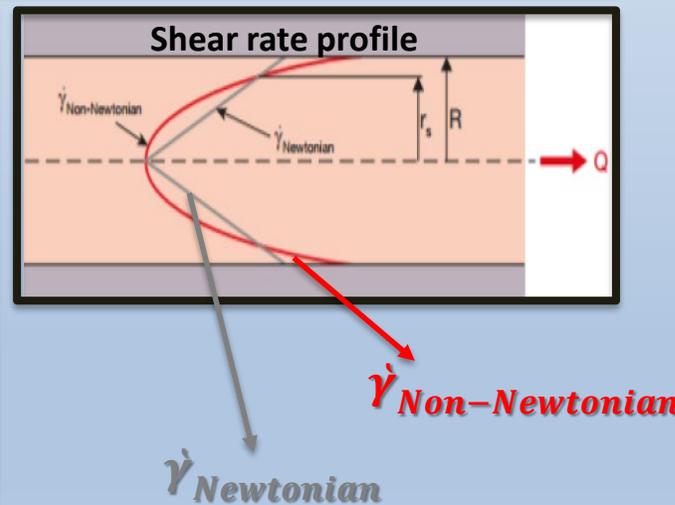
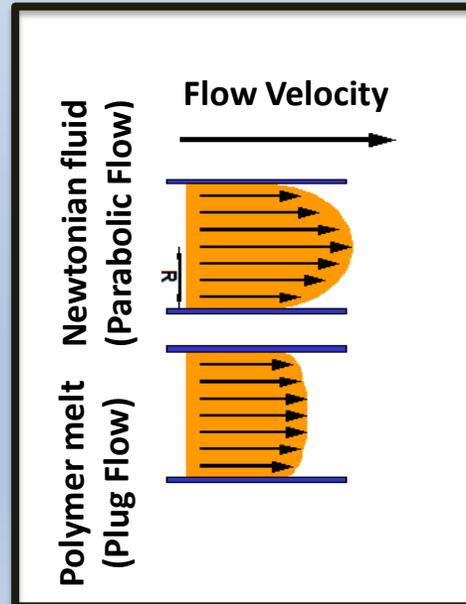
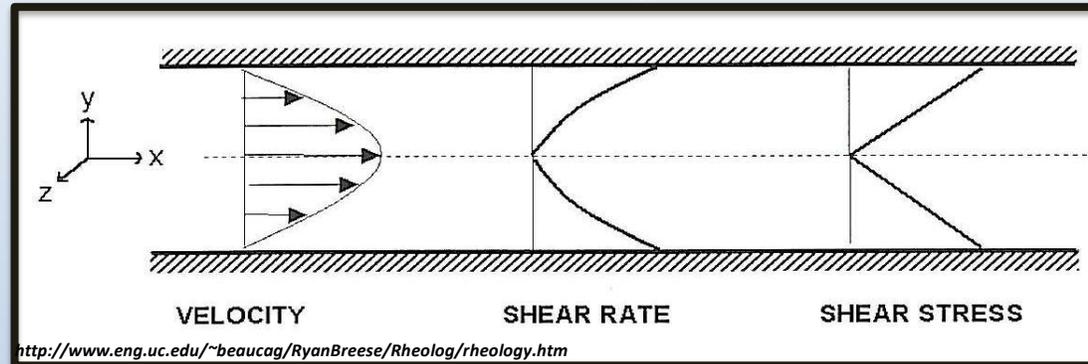
# Rabinowicz and Bagley Corrections

# Corrections

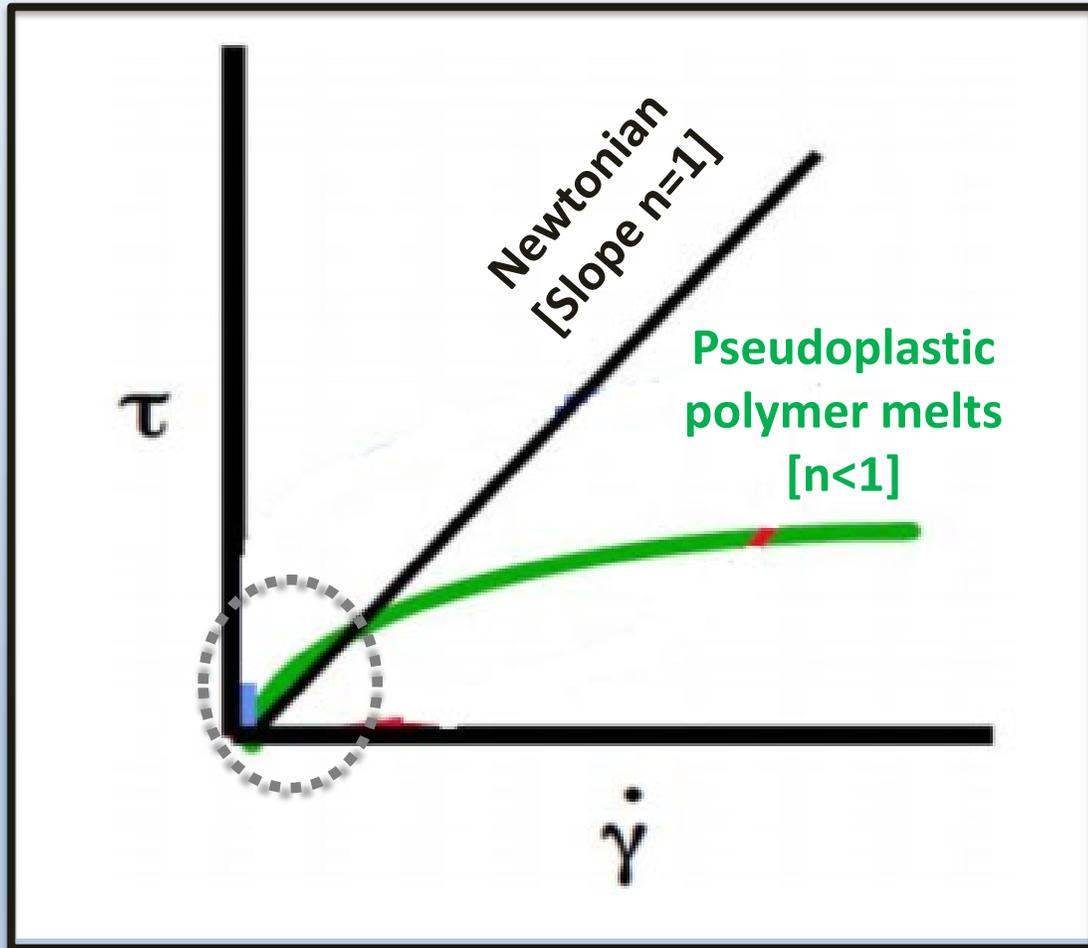
- ❖ All calculations we discussed are “Apparent” values since they assume Newtonian behavior and that the entire pressure drop occurs inside through die. (Assuming no die entrance/exit effect)
- ❖ **Rabinowicz correction** needs to be applied in order to rectify the data for non-Newtonian character of polymer melt. (Calculation of **corrected shear rate**)
- ❖ **Bagley correction** needs to be applied to consider the extra pressure drop that may happen at the entrance/exit of the die.(Calculation of **corrected shear stress**)

# Why Rabinowicz Corrections?

## Flow through a die



# Rabinowicz Corrections

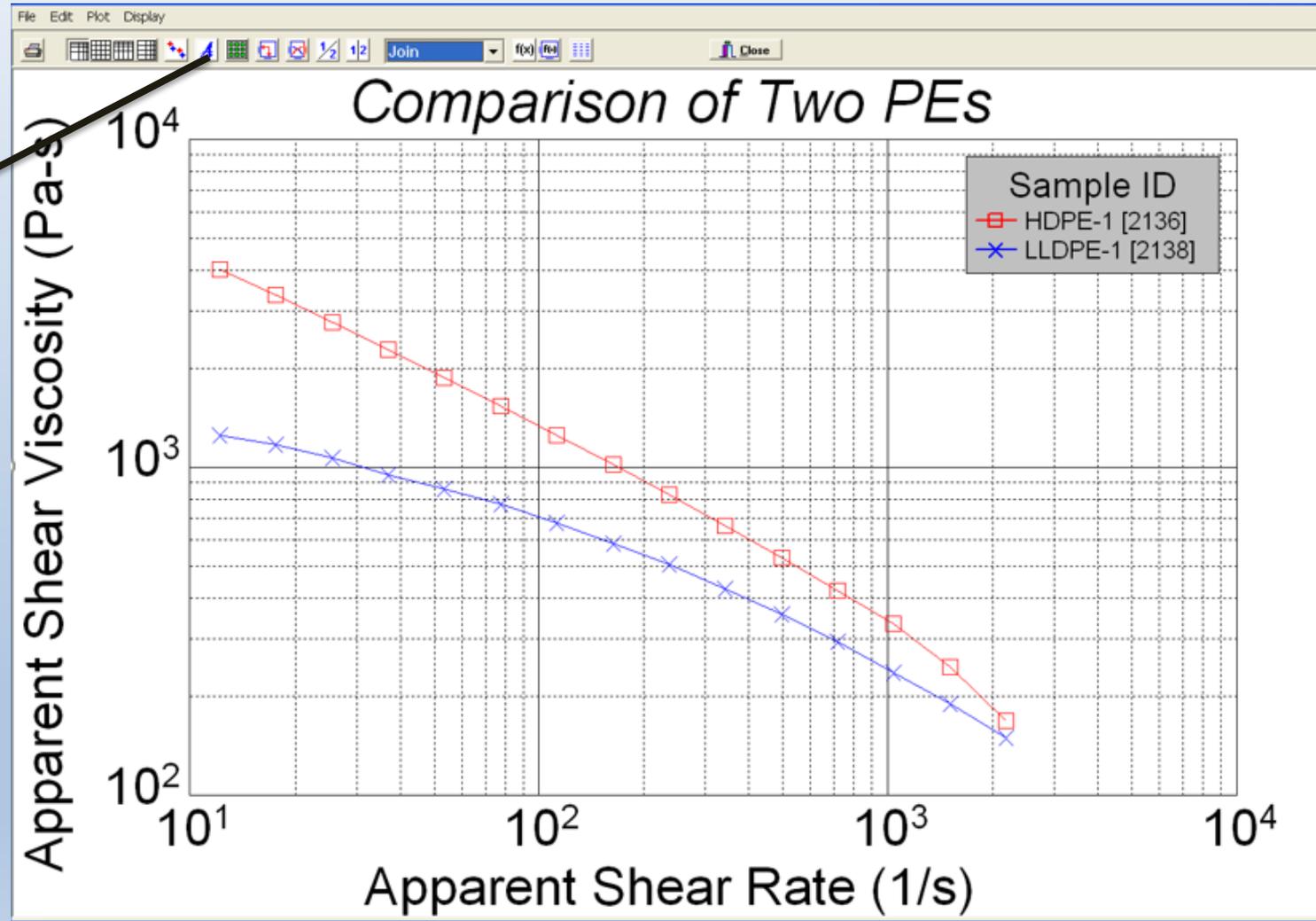


$$\dot{\gamma}_{corrected} = \left( \frac{3n + 1}{4n} \right) \dot{\gamma}_{apparent}$$

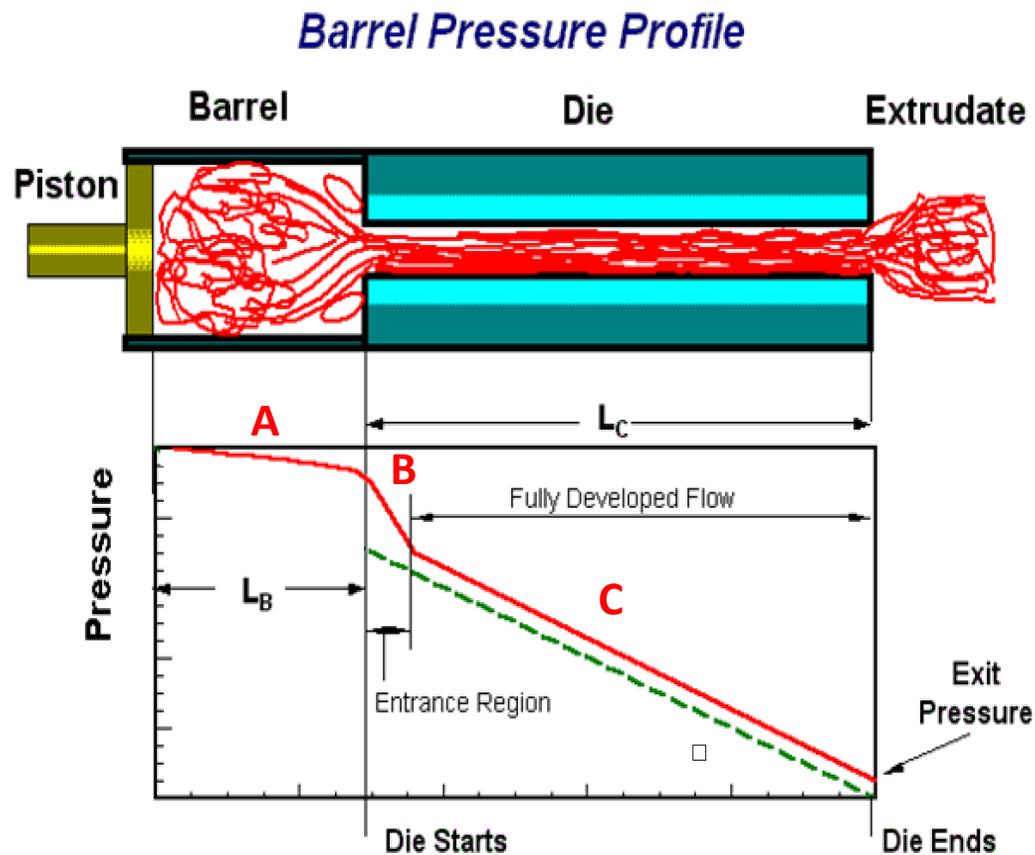
Correction Factor

# How to Apply Rabinowicz Corrections in LabKars?

Click to plot viscosity  
versus “corrected”  
shear rate



# Why Bagley Corrections?



- **$A = \Delta p_{Barrel}$** : Very minor pressure drop in barrel
- **$B = \Delta p_{Entrance}$** : Excess pressure drop in die entrance
- **$C = \Delta p_{Capillary}$** : Fully developed flow region in capillary die

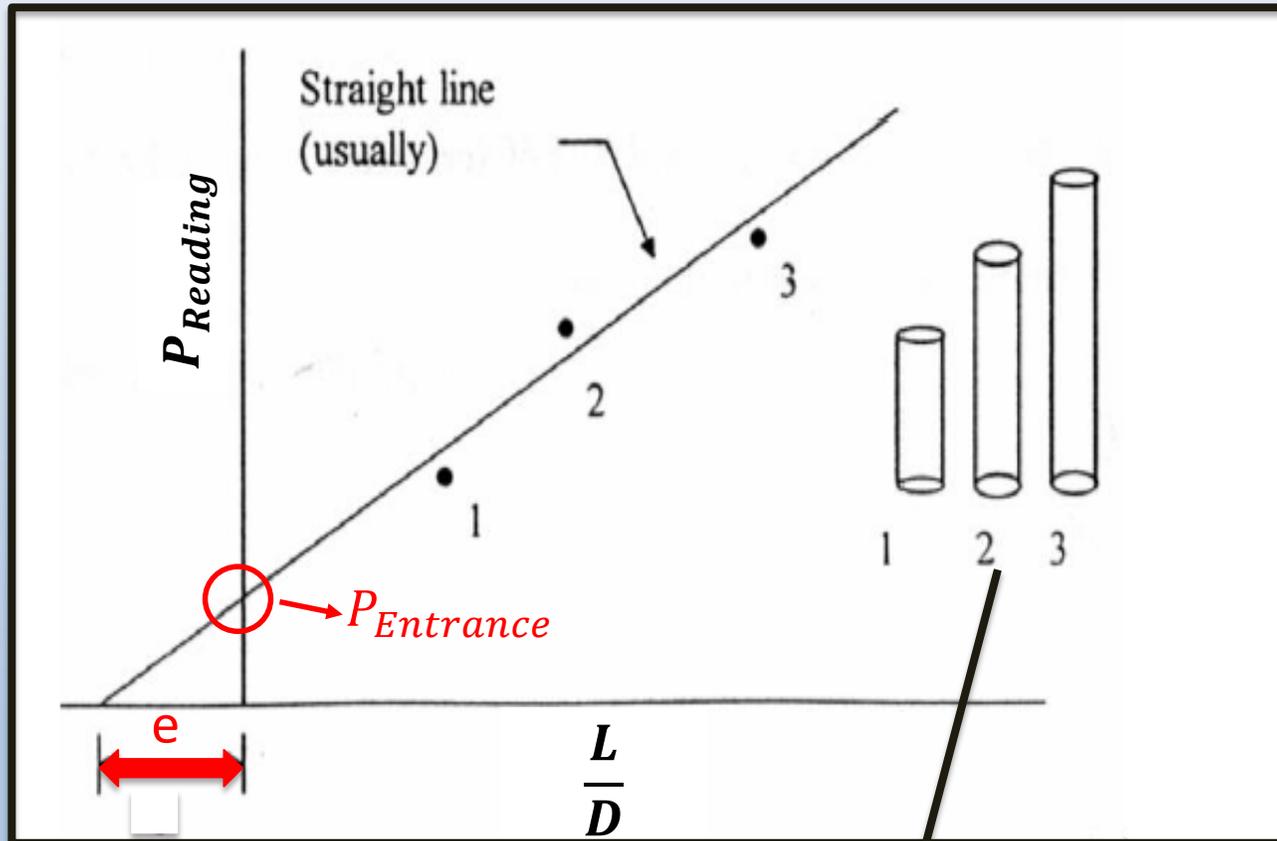
- ❖ Large pressure drop associated with the flow entrance region due to viscoelasticity of polymers.
- ❖ After entrance region, The pressure gradient approaches a constant value (fully developed flow region)

❖ In reality:

$$\Delta P_{total} = \Delta P_{Entrance} + \Delta P_{capillary}$$

- ❖ Bagley correction needs to be applied to calculate the entrance pressure drop

# How to Calculate the Entrance Pressure?



Three dies, same diameter  
but different lengths  
(e.g. L/D: 10, 20, and 30)

$$\tau_{Corrected} = \frac{P_{Reading} - P_{Entrance}}{4\left(\frac{L}{D}\right)}$$

where

$$P_{Entrance} = P \left( \text{at } \frac{L}{D} = 0 \right)$$

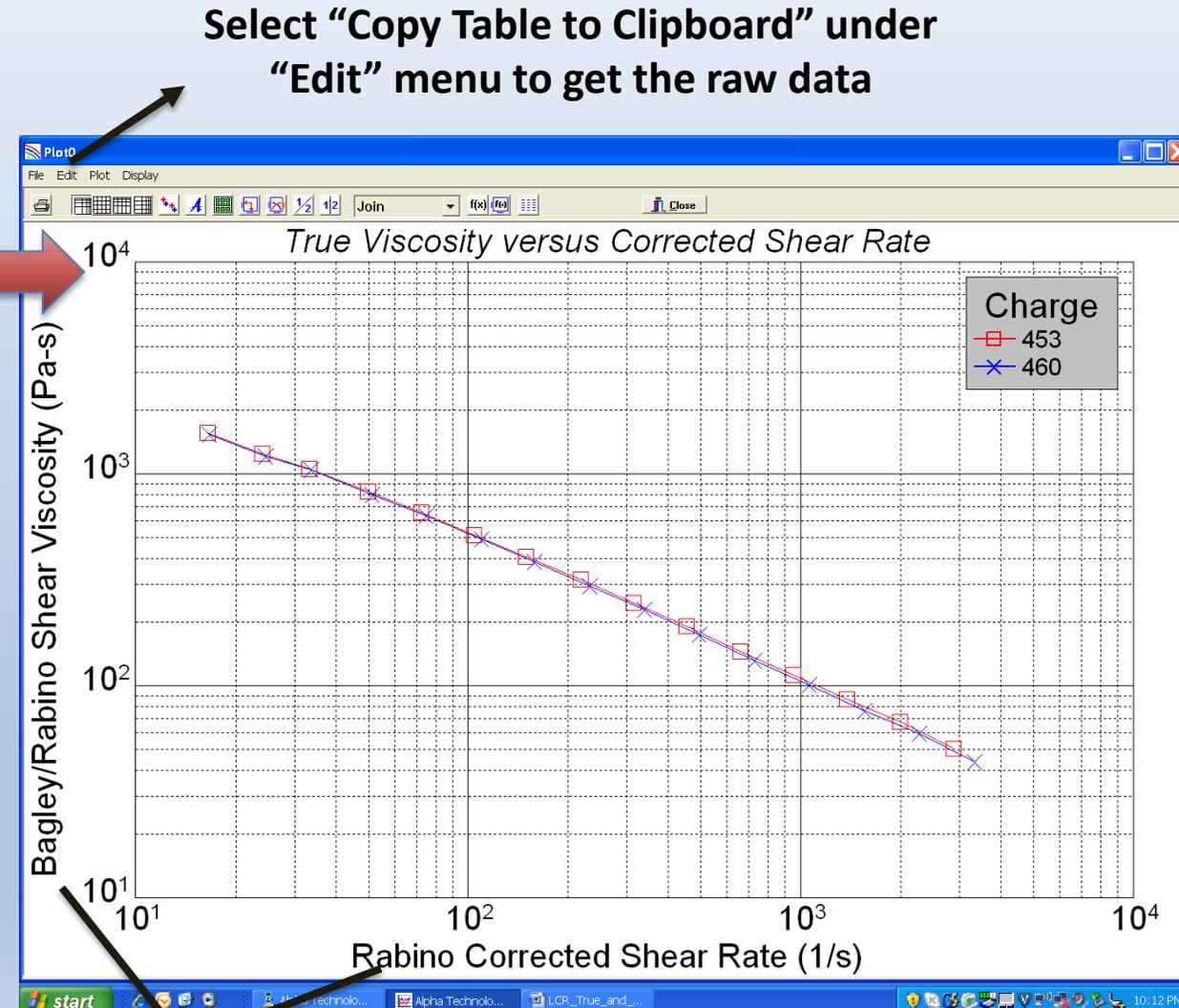
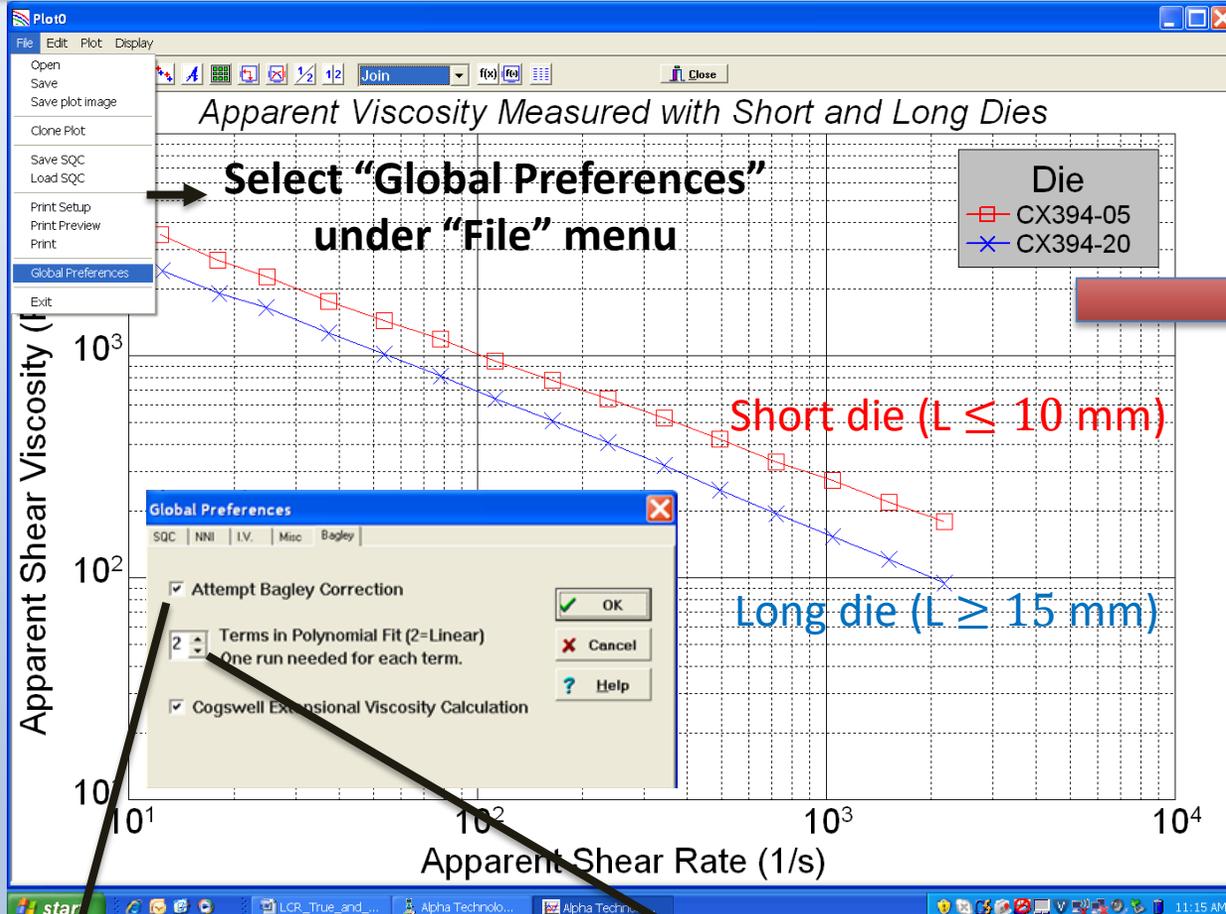
OR

$$\tau_{Corrected} = \frac{P_{Reading}}{4\left(\frac{L}{D} + e\right)}$$

where

$$e = \text{end correction} = \frac{-L_{Entrance}}{D}$$

# How to Apply Bagley Corrections in LabKars?



Select "Attempt Bagley Correction"

Insert number "2"

Right click on each axis and select the appropriate item to plot



# How to Calculate True Viscosity?

$$\eta_{True} = \frac{\tau_C}{\dot{\gamma}_C}$$

where

- $\eta_{True}$  (Pa-s): Viscosity with Bagley and Rabinowicz Corrections
- $\tau_C$  (Pa): Bagley corrected shear stress
- $\dot{\gamma}_C$  (1/s): Rabinowicz corrected shear rate



*From lab to production,  
providing a window into the process*

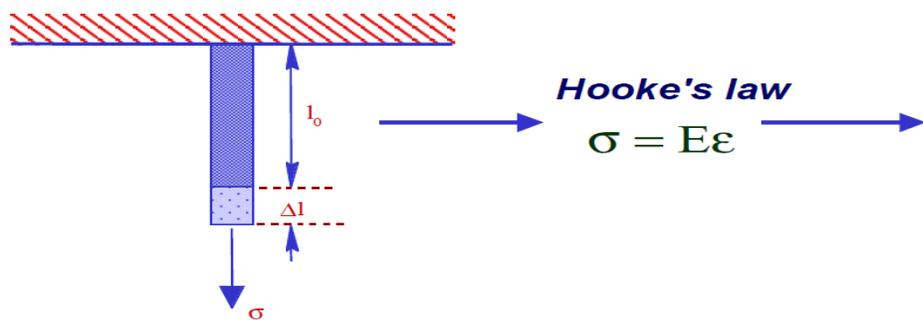
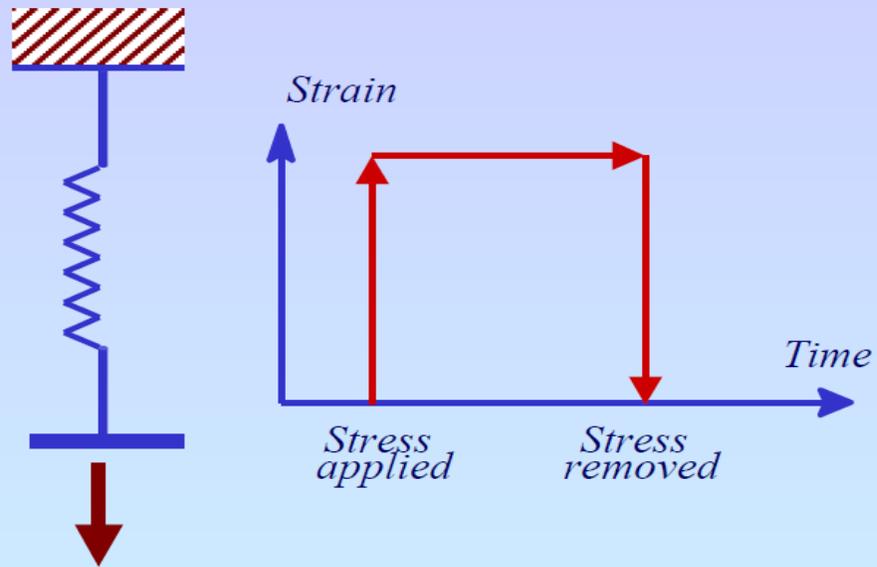


# Viscoelasticity

# Mechanical Models of Viscoelastic Behavior

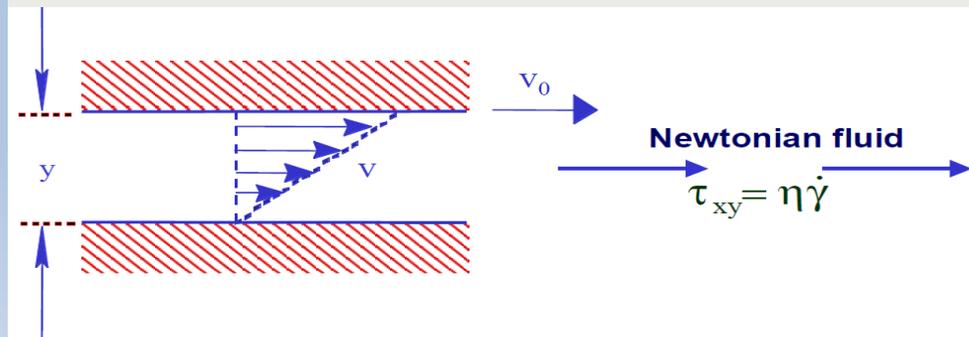
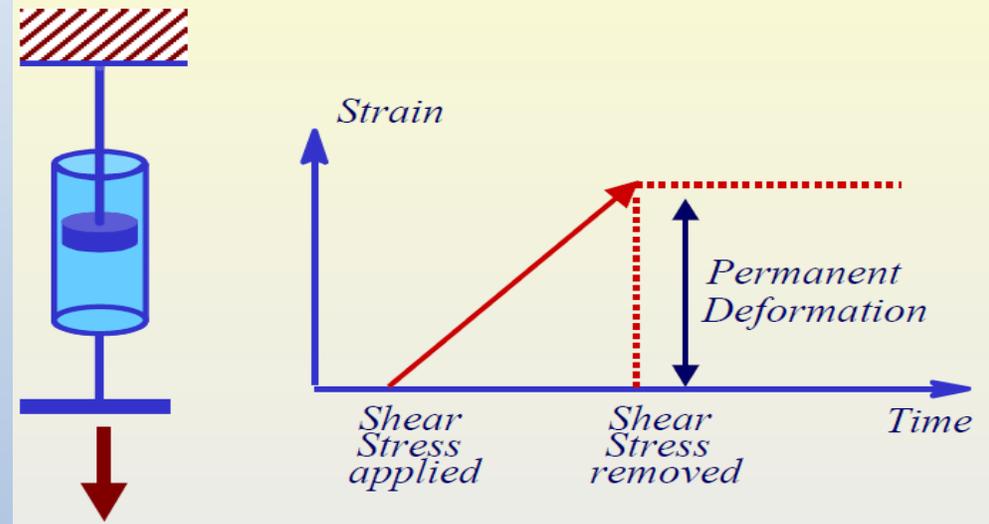
## PURELY ELASTIC RESPONSE

$$\sigma = E\varepsilon$$

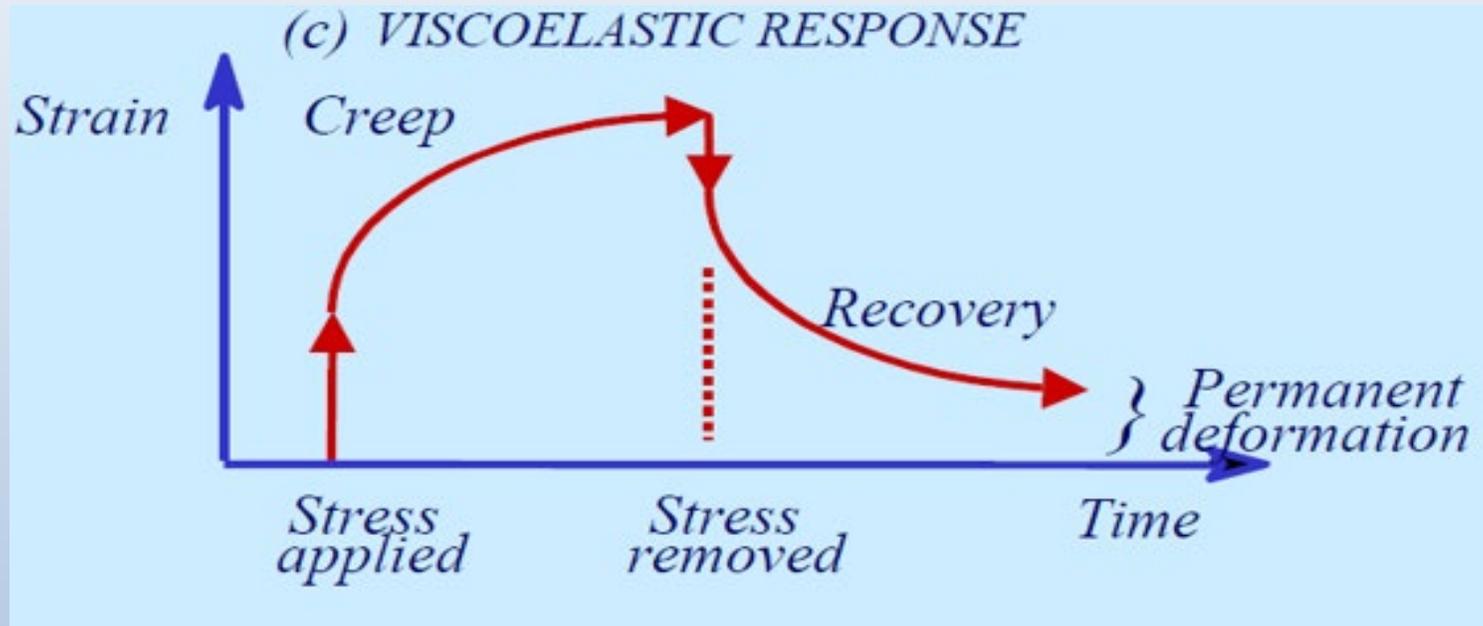


## PURELY VISCOUS RESPONSE

$$\sigma = \eta \frac{d\varepsilon}{dt}$$



# Mechanical Models of Viscoelastic Behavior





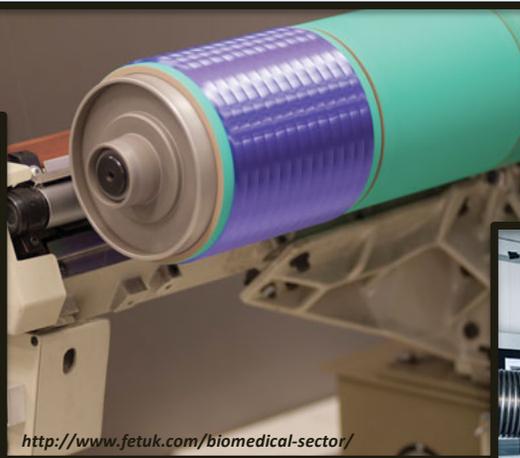
*From lab to production,  
providing a window into the process*



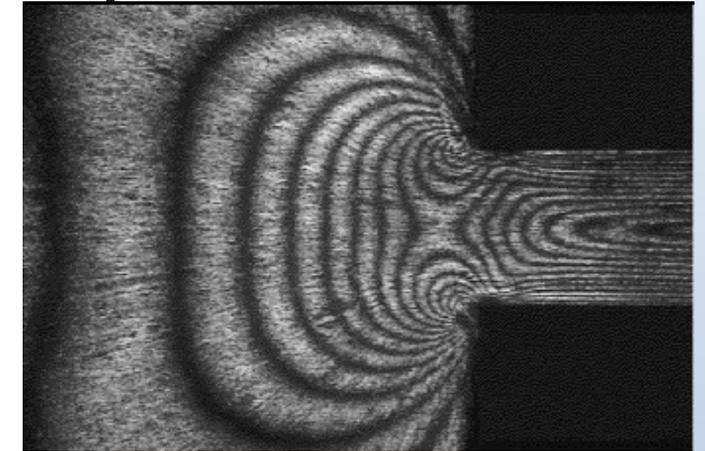
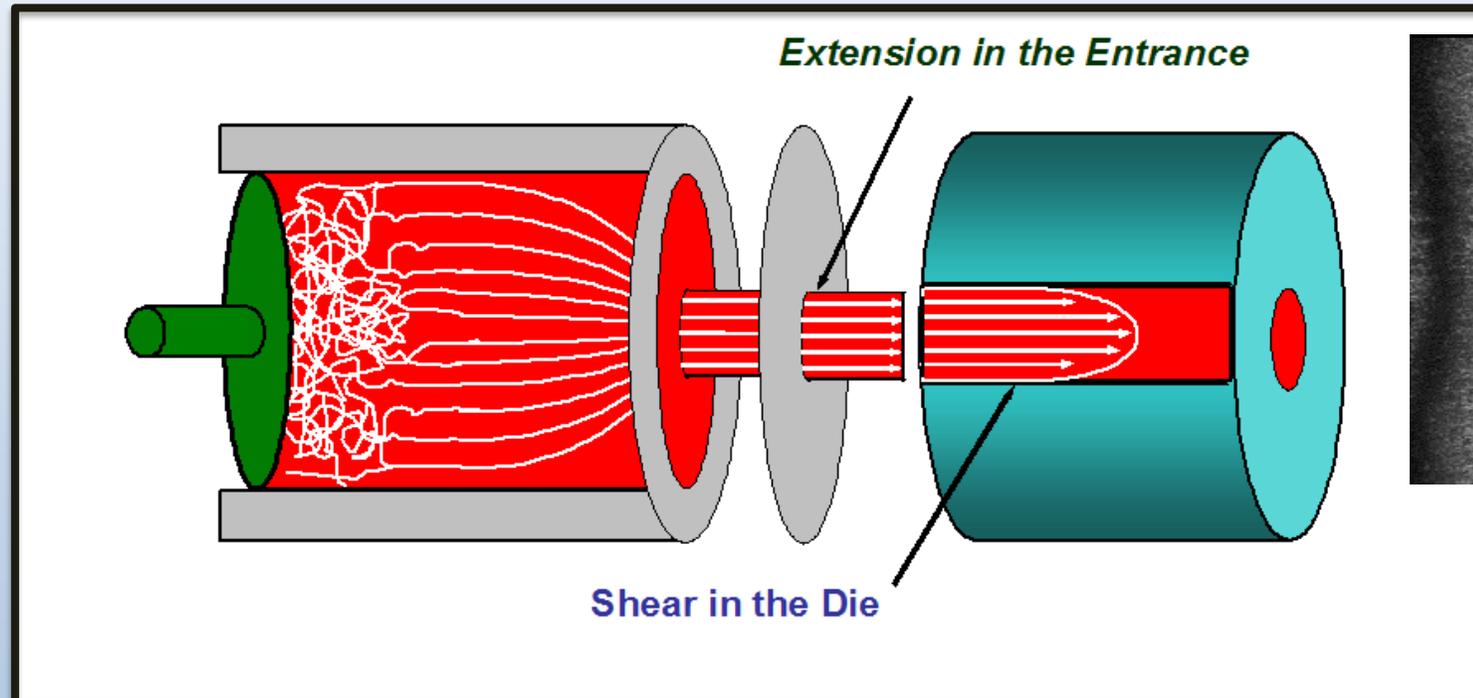
# Extensional Viscosity Measurements

# When Extensional Viscosity is important?

Any process that has stretch!



# What is Extensional (Elongational) Viscosity?



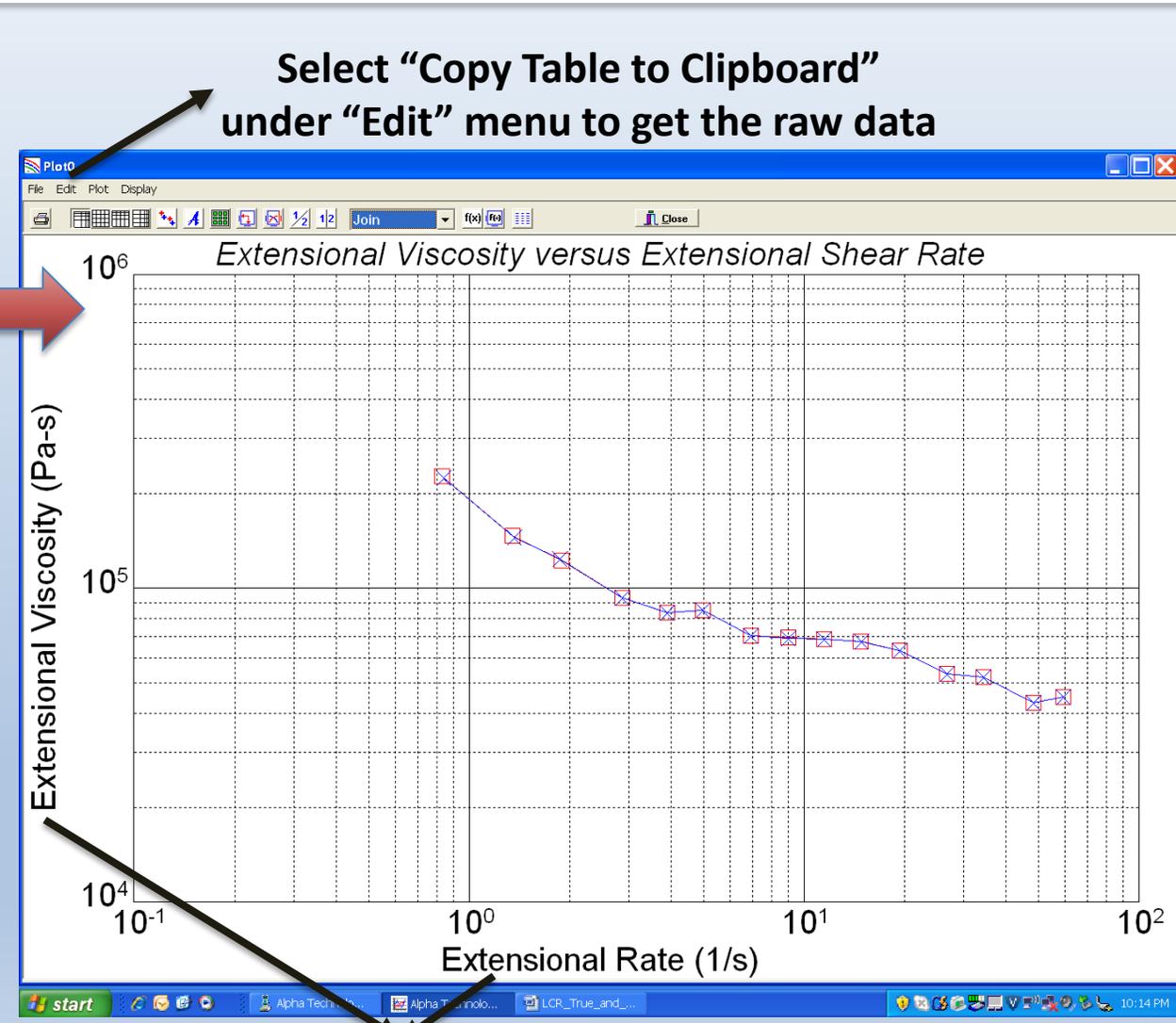
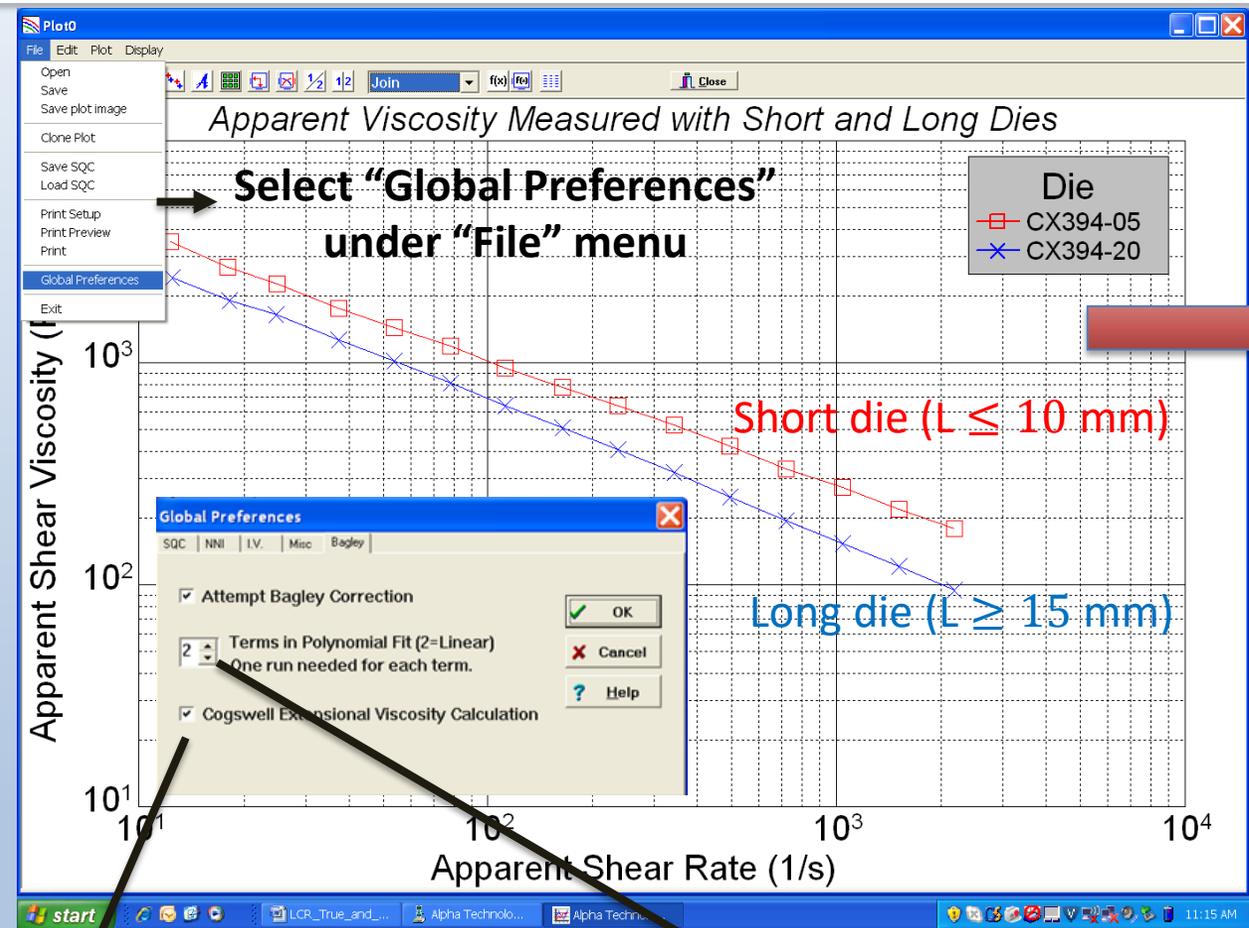
- ❖ Since the diameter of the barrel versus die is very large, there is a high degree of stretching along streamlines at the entrance to the die
- ❖ Cogswell assumes that the pressure drop in entrance has two components, one due to shear and one due to extension

# Cogswell's Equations

<b>Extensional Stress</b>	$\diamond \sigma_{Ext} = \frac{3}{8} (n + 1) P_{Ent}$	<ul style="list-style-type: none"><li>➤ <math>\sigma_{Ext}</math> (Pa): Extensional stress</li><li>➤ <math>n</math>: Power law index</li><li>➤ <math>P_{Ent}</math> (Pa): Entrance pressure</li></ul>
<b>Extensional Rate</b>	$\diamond \dot{\epsilon} = \frac{4\dot{\gamma}_a^2 \eta_a}{3(n+1)P_{Ent}}$	<ul style="list-style-type: none"><li>➤ <math>\epsilon</math> (1/s): Extensional rate</li><li>➤ <math>\dot{\gamma}_a</math> (1/s): Apparent shear rate</li><li>➤ <math>P_{Ent}</math> (Pa): Entrance pressure</li></ul>
<b>Extensional Viscosity</b>	$\diamond \eta_{Ext} = \frac{9(n+1)^2 P_{Ent}^2}{32\eta_a \dot{\gamma}_a^2}$	<ul style="list-style-type: none"><li>➤ <math>\eta_{Ext}</math> (Pa-s): Extensional viscosity</li></ul>

J.M. Dealy, K.F. Wissbrun, *Melt Rheology and its Role in Plastics Processing: Theory and Applications*, Van Nostrand Reinhold, New York (1990).

# How to Perform Extensional Viscosity Measurements in LabKars?



Select "Copy Table to Clipboard" under "Edit" menu to get the raw data

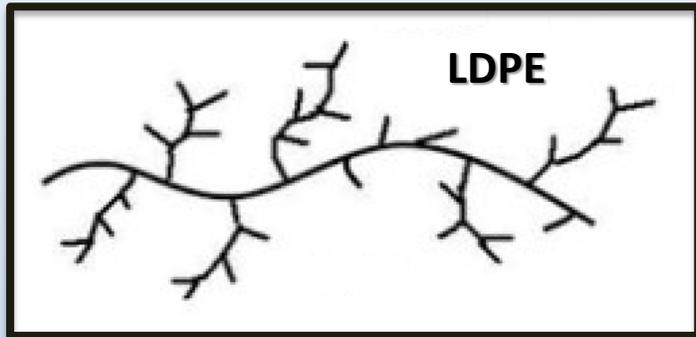
Select "Cogswell Extensional Viscosity Calculation"

Insert number "2"

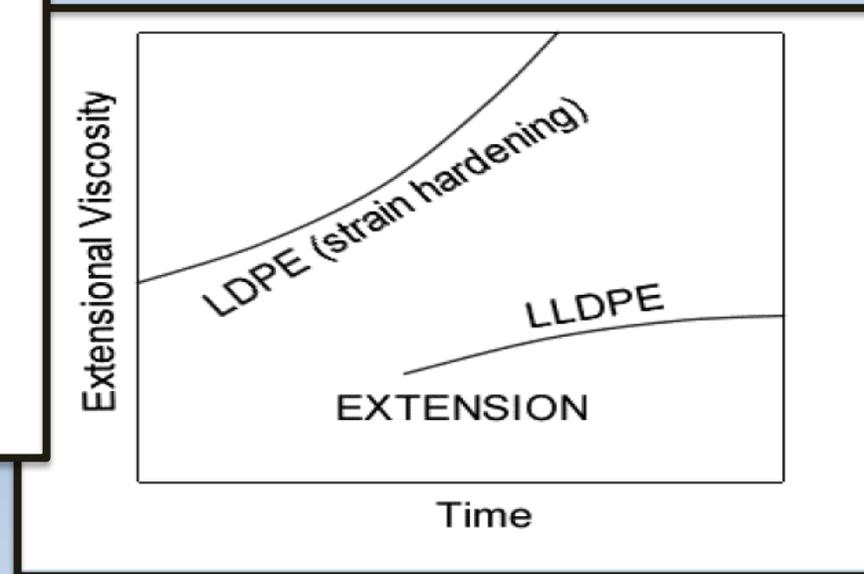
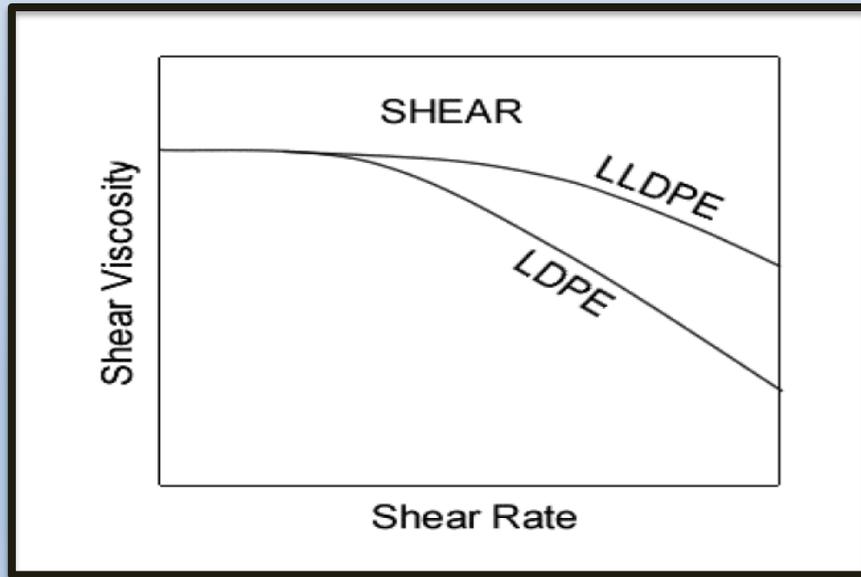
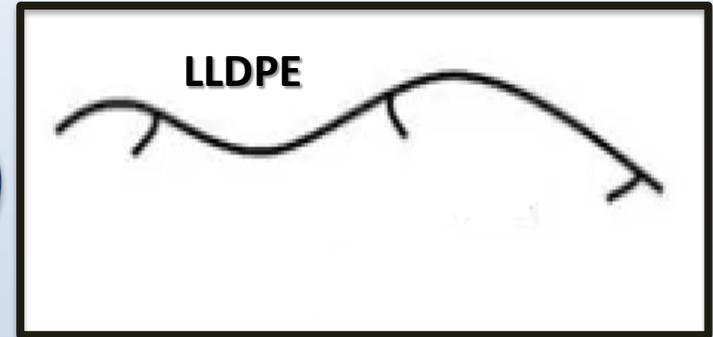
Right click on each axis and select the extensional type of axis



# Example!



LLDPE (Linear structure) is stiffer than LDPE (branched structure) in shear but softer in extension



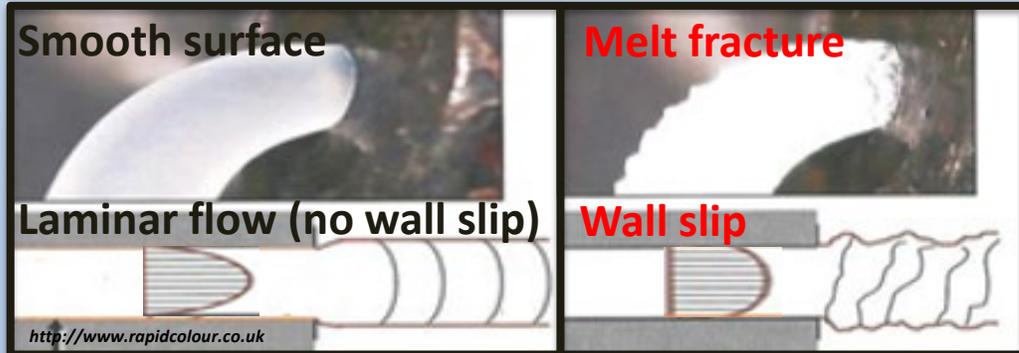
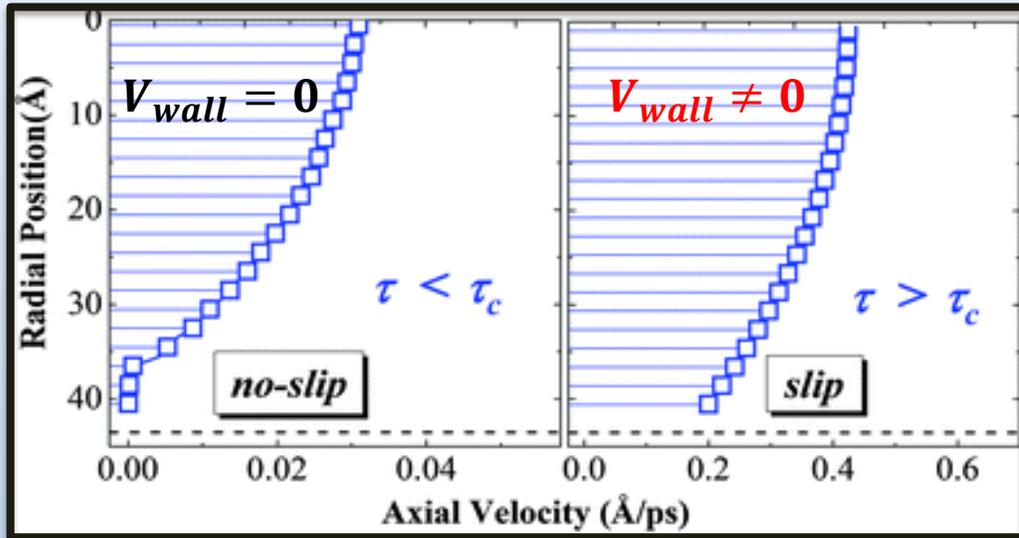


From lab to production,  
providing a window into the process



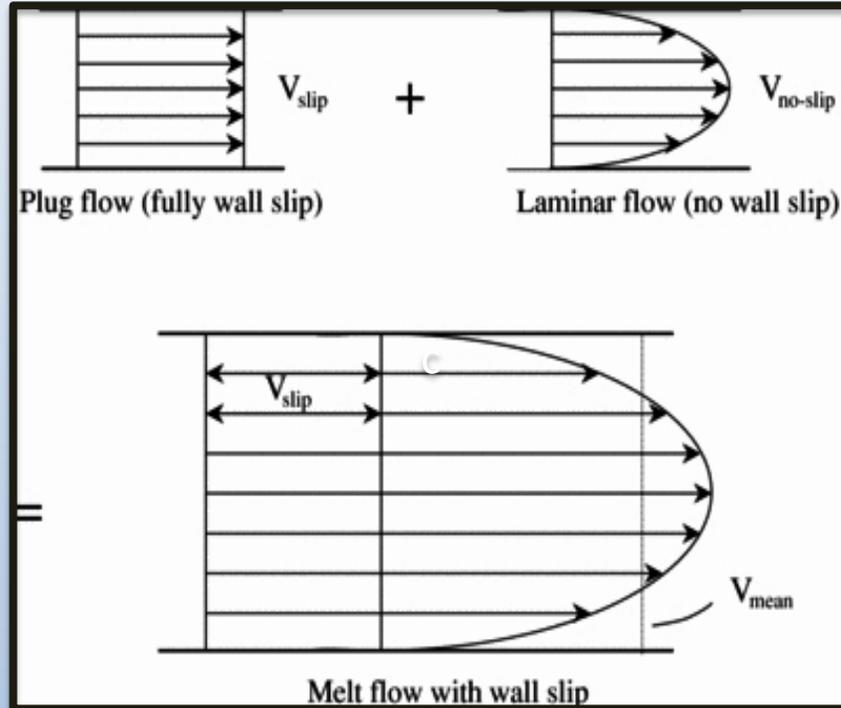
# Wall Slip Velocity & Melt Fracture

# Wall Slip in Capillary Flow

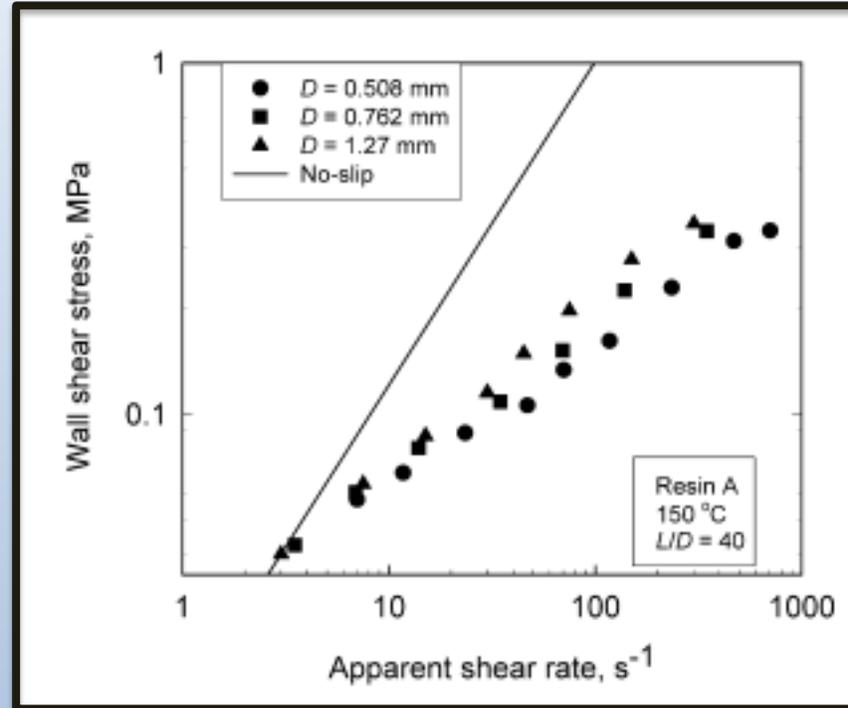


- ❖ Wall slip velocity increases dramatically above critical shear stress ( $\sim 0.1$  MPa).
- ❖ Slippage reduces apparent viscosity. Also, the surface of the extrudate begins to be rough (**melt fracture**).
- ❖ Wall slip happens due to elastic properties of polymer materials.
- ❖ Critical shear stress is lower for polymers with higher molecular weight
- ❖ Trouble shooting by using larger die diameter, longer die, tapering the die, higher temperature, or lower shear rate.

# Effect of Wall Slip on Capillary Rheometer Results



R.D. Chien, W.R. Jong, S.C. Chen, Study on Rheological Behavior of Polymer Melt Flowing Through Micro-Channels Considering the Wall-Slip Effect, *J. Micromech. Microeng.* 15, (2005), 1389



S. G. Hatzikiriakos, Wall Slip of Molten Polymers, *Progress in Polymer Science*, 37 (2012), 624-643

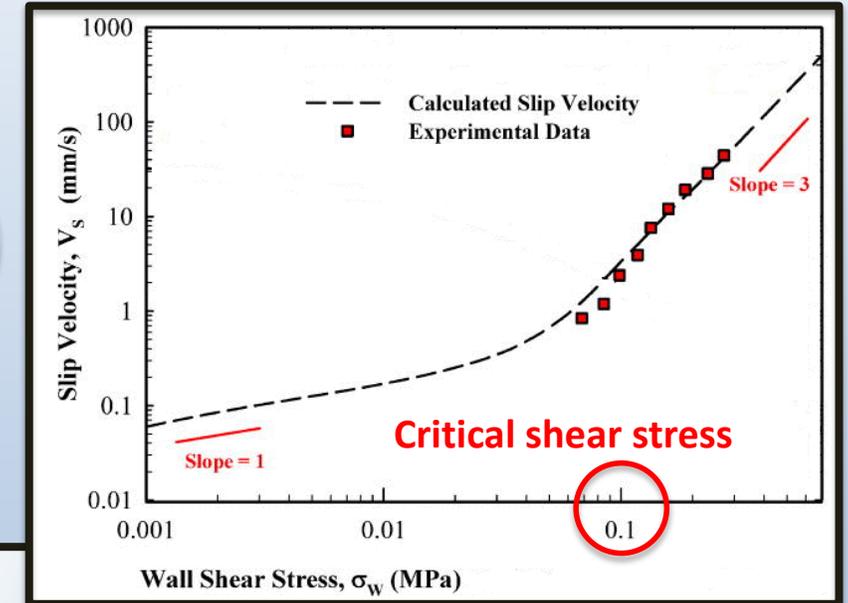
Wall slip causes formation of plug flow and a discontinuity in flow curve.

# How to Calculate Wall Slip Velocity?

$$\dot{\gamma}_a = 4V_w \left( \frac{1}{R_C} \right) + X$$

where

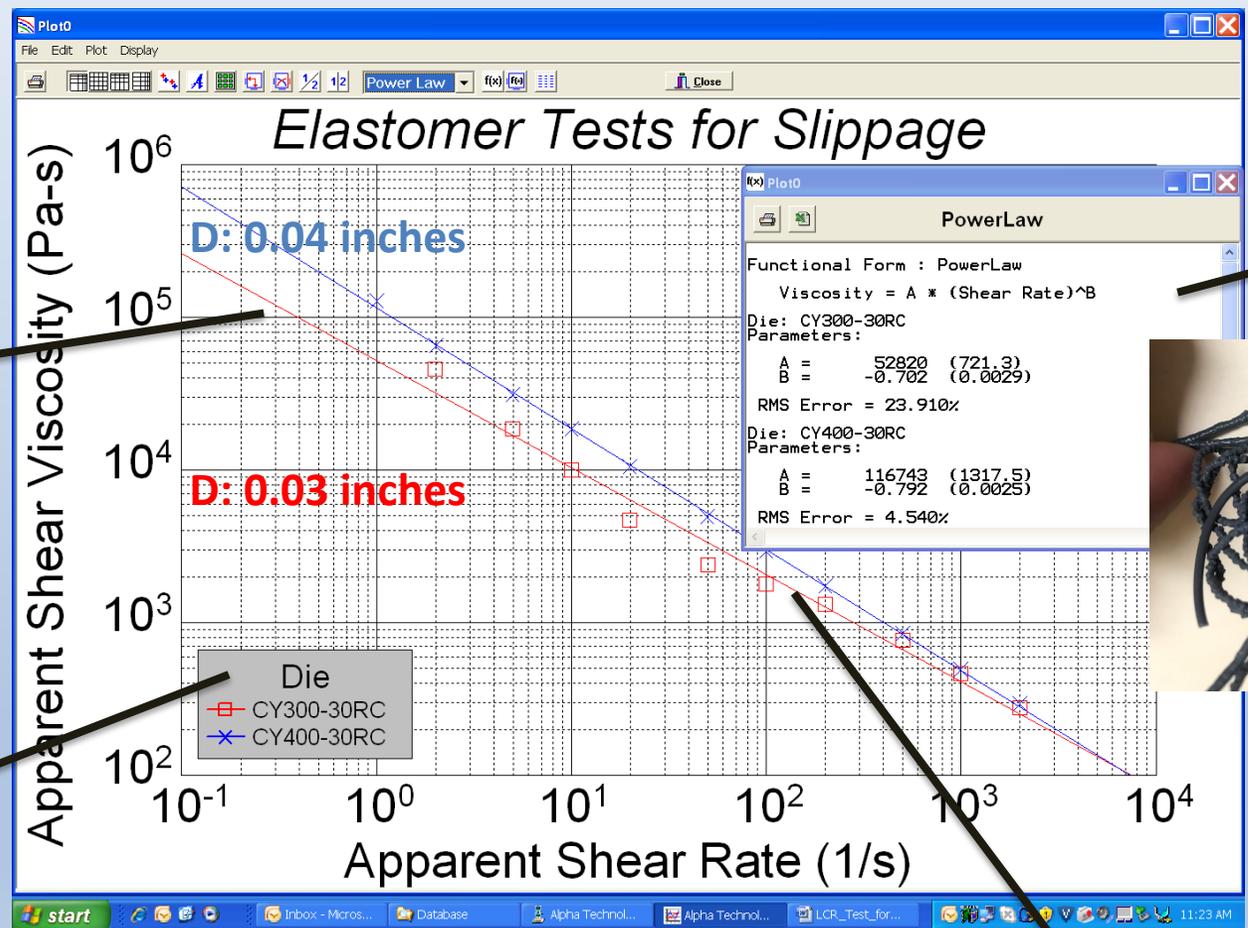
- $V_w$  (mm/sec): Wall slip velocity
- $\dot{\gamma}_a$  (1/s): apparent shear rate at a given value of shear stress
- $R_C$  (mm): Capillary die radius
- $X$ : Dimensionless parameter (a function of the shear stress)



## Steps:

1. Produce a series of flow curves using a set of dies of varying radius ( $R_C$ ).
2. At a given value of shear stress, make a plot of apparent shear rate ( $\dot{\gamma}_a$ ) versus inverse radius ( $\frac{1}{R_C}$ ).
3. Slip velocity at a given shear stress will be one quarter of the slope of  $\dot{\gamma}_a$ -vs- $\frac{1}{R_C}$  plot.
4. Repeat the test at other shear stresses and calculate the slip velocity at each specific shear stress.
5. Make the plot of slip velocity versus shear stress.

# How to Notice Wall Slippage from Flow Curve in LCR?



NOT overlapping of results from two dies means slippage happened at the smaller die

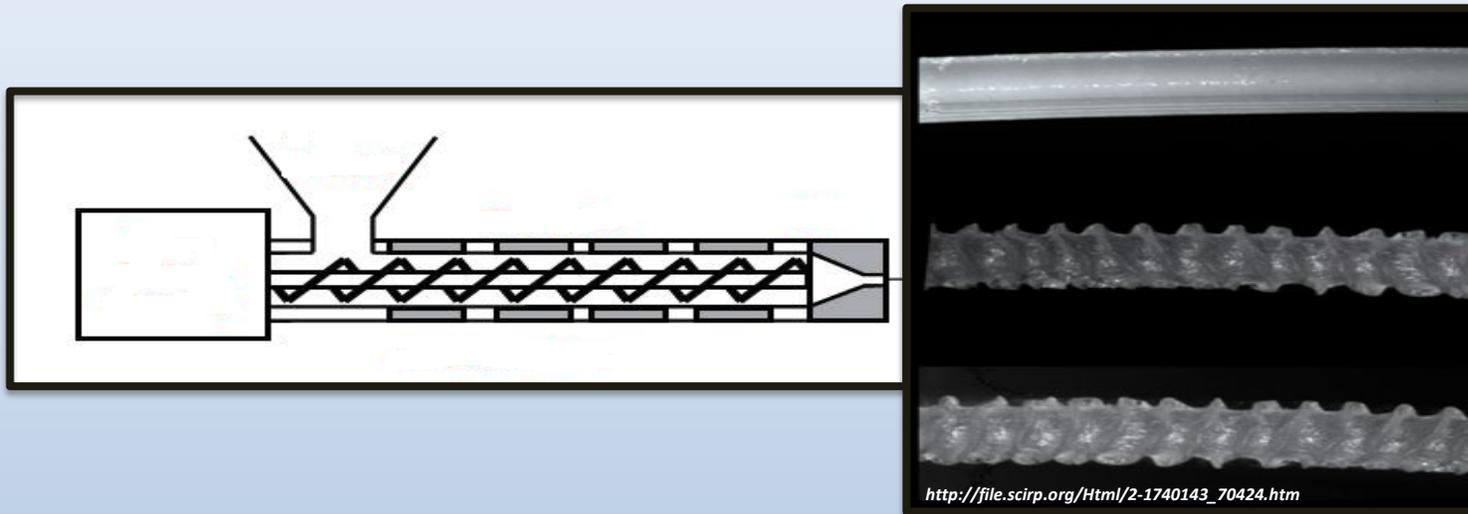
Slippage affect Power-Law model parameters



Perform shear rate sweep on two dies with same L/D but different diameters

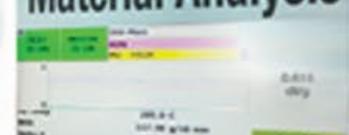
Viscosity is lower when slippage happens in smaller die diameter.

# Melt Fracture Trouble Shooting in Extrusion Process



This phenomena happens due to elasticity of polymer melts. **Any procedure that reduces the melt elasticity will help to troubleshoot.** e.g.:

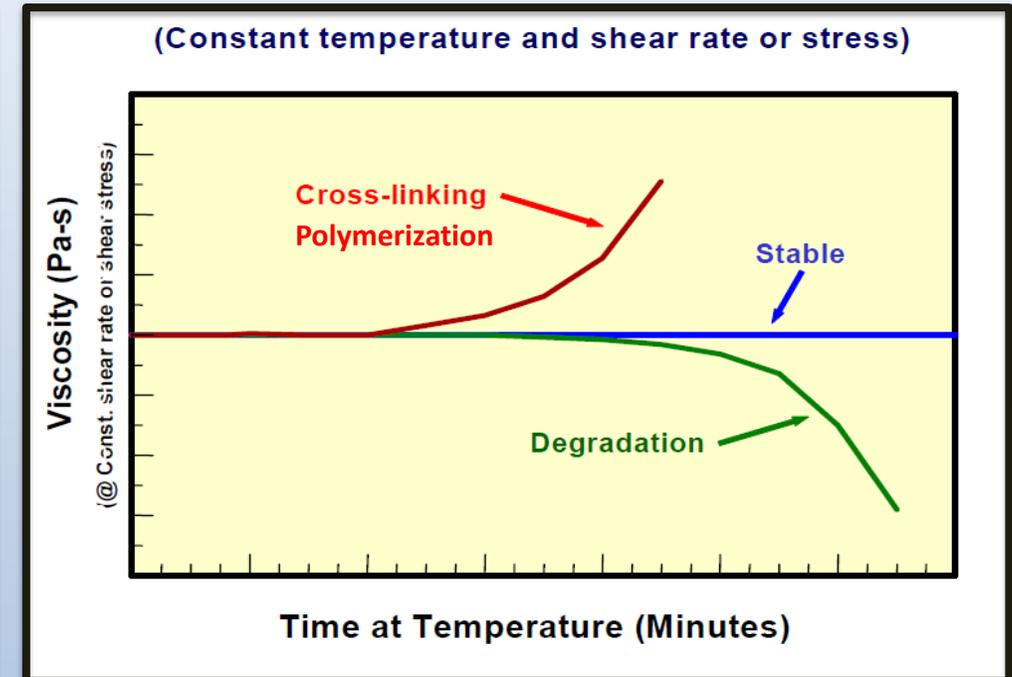
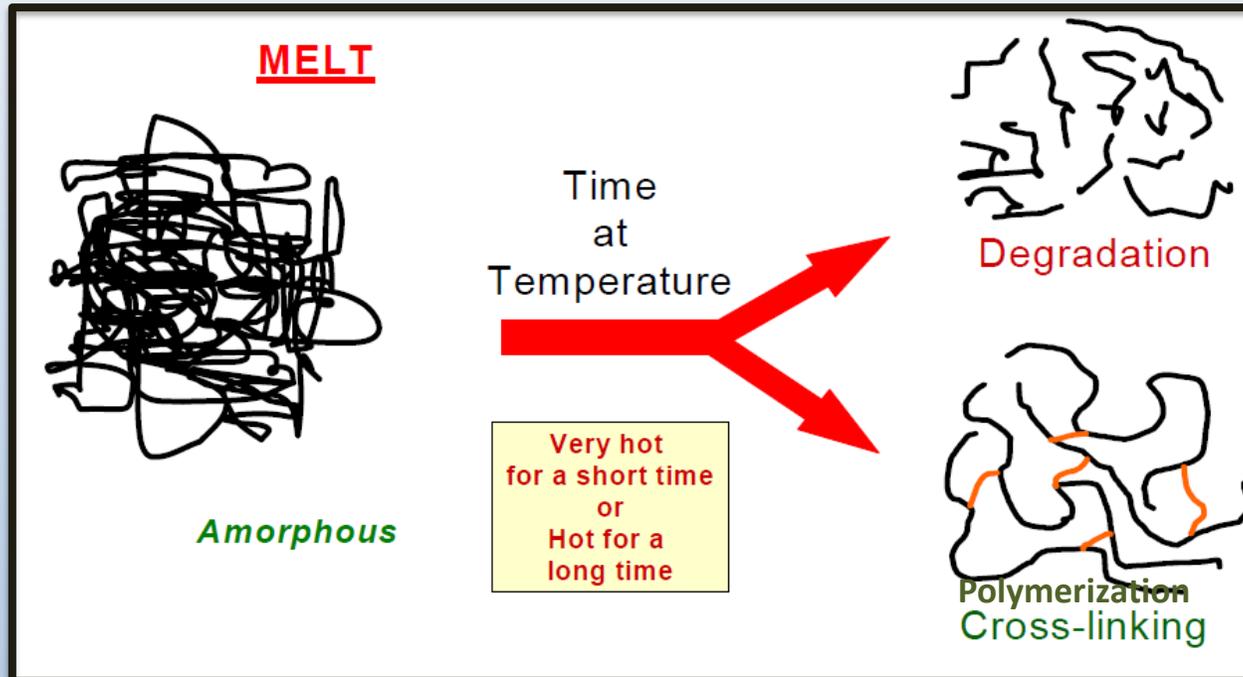
- ✓ Increasing temperature
- ✓ Reducing screw speed (shear rate)
- ✓ Increasing the die length or die diameter
- ✓ Tapering the die



# Time Sweep Test

(Thermal Stability of Polymers)

# Thermal Stability of Polymer Melt



- ❖ The stability test can determine the resistance of a material to a change in viscosity at the test temperature.
- ❖ The stability of polymer melts varies depending on temperature, time at temperature, formulation, and contaminants.
- ❖ This test can be used to show the presence of moisture or reactive chemicals in a polymer.
- ❖ This test can be used to measure the degradation rate or reactivity of a sample

# How to Set up Thermal Stability Test (Time Sweep) in LabKars?

**Setup**

**Data Point Setup # 11**

Setup #	Program Name	Start Pos.	Temperature	Melt Time	Sensor1 ID	Die
2	7523 Control Grey PP	100	100	230	300 LC-103N	CY300-33
3	Polycarbonate	100	300	300	300 LC-103N	CY300-33
4	Position Based Test	90	190	300	300 LC-103N	CX300-33
5	Bagley Test	100	230	300	PT-142BAR-A	CX394-40
6	Thermalstability Test	100	285	120	LC-103N	CZ600-20
7	Nylon	90	240	240	LC-103N	CZ394-20
8	HDPE	90	90	360	LC-103N	CZ787-15
9	PEEK	100	400	300	LC-103N	CY400-15
10	PET I.V.	100	285	240	LC-103N	CX300-33
11	Nylon Stability	89	240	180	LC-502N	CZ394-20

Control Mode:  Rate  Stress

Test Type:  Steady State  Position (Acquire At - mm)  Manual  Time Delay (Acquire At - sec)  Elapse Time (Acquire At - sec)

Minimum Speed: 0.03  
Maximum Speed: 650

Point #	Speed Control	Shear Rate	Delay Sec	Time Min	Acquire At-mm
1	6.50	79.05			102.0
2	6.50	79.05			115.0
3	6.50	79.05			128.0
4	6.50	79.05			141.0
5	6.50	79.05			154.0
6	6.50	79.05			167.0
7	6.50	79.05			180.0
8	6.50	79.05			193.0
9	6.50	79.05			206.0
10	6.50	79.05			219.0

Select "Position" Test Type

- $\Delta L = S \times \Delta t$
- 13 mm    6.5 mm/sec    2 sec
- Where
- $\Delta L$ : Piston travel distance between points
  - $S$ : Piston speed  
 $= \frac{\text{Max plunger travel (130 mm)}}{\text{Test time (e.g. 20 min)}}$
  - $\Delta t$ : Piston time travel between points  
 $= \frac{\text{Test time (e.g. 20 min)}}{\text{\# of points (e.g. 10)}}$

Applying the same speed and shear rate multiple times

# How to Set up Thermal Stability Test (Time Sweep) in LabKars?

**Setup**

**Data Point Setup # 11**

Setup #	Program Name	Start Pos.	Temperature	Melt Time	Sensor1 ID	Die
2	7523 Control Grey PP	100	230	300	LC-103N	CY300-33
3	Polycarbonate	100	300	300	LC-103N	CY300-33
4	Position Based Test	90	190	300	LC-103N	CX300-33
5	Bagley Test	100	230	300	PT-142BAR-A	CX394-40
6	Thermalstability Test	100	285	120	LC-103N	CZ600-20
7	Nylon	90	240	240	LC-103N	CZ394-20
8	HDPE	90	90	360	LC-103N	CZ787-15
9	PEEK	100	400	300	LC-103N	CY400-15
10	PET I.V.	100	285	240	LC-103N	CX300-33
11	Nylon Stability	89	240	180	LC-502N	CZ394-20

Control Mode  
 Rate  Stress

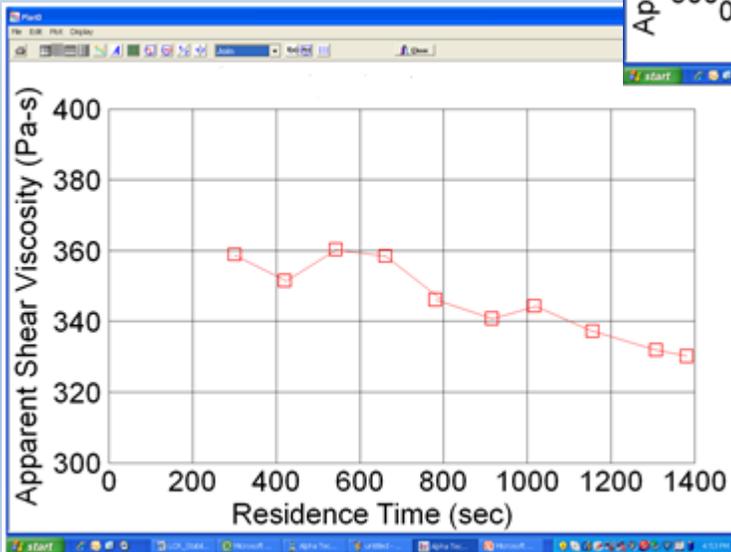
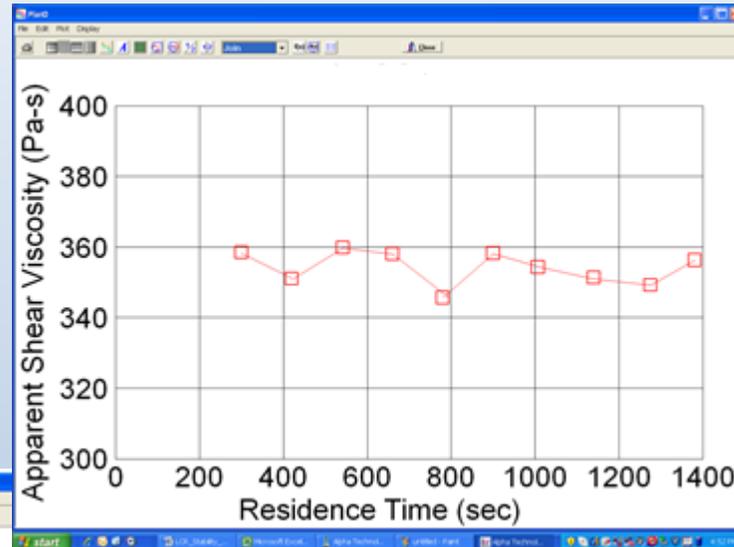
Test Type  
 Steady State  
 Position (Acquire At - mm)  
 Manual  
 Time Delay (Acquire At - sec)  
 Elapse Time (Acquire At - sec)

Minimum Speed   
Maximum Speed

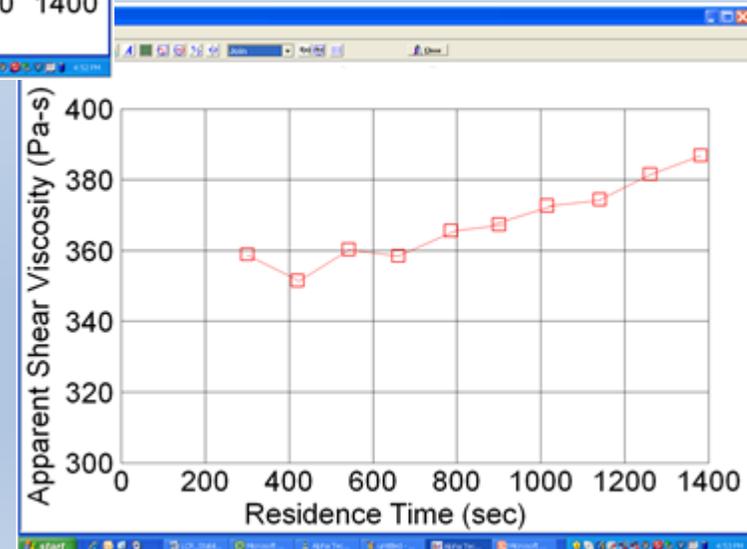
Point #	Speed Control	Shear Rate	Delay Sec	Time Min	Acquire At-mm
1	6.50	79.05			102.0
2	6.50	79.05	66		115.0
3	6.50	79.05	66		128.0
4	6.50	79.05	66		141.0
5	6.50	79.05	66		154.0
6	6.50	79.05	66		167.0
7	6.50	79.05	66		180.0
8	6.50	79.05	66		193.0
9	6.50	79.05	66		206.0
10	6.50	79.05	66		219.0

**Add delay time to increase the stability test time while keeping shear rate constant**

# Thermal Stability Test Results (Time Sweep) in LabKars



**Plot of apparent viscosity versus residence time**





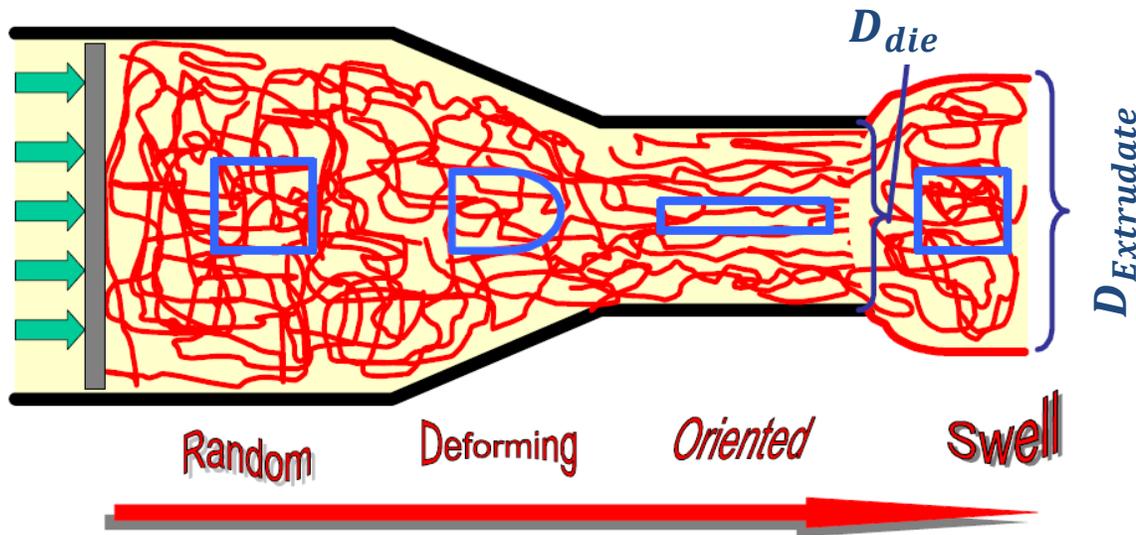
*From lab to production,  
providing a window into the process*



# Die Swell

# Die swell Ratio

## The Source of Extrudate Swell

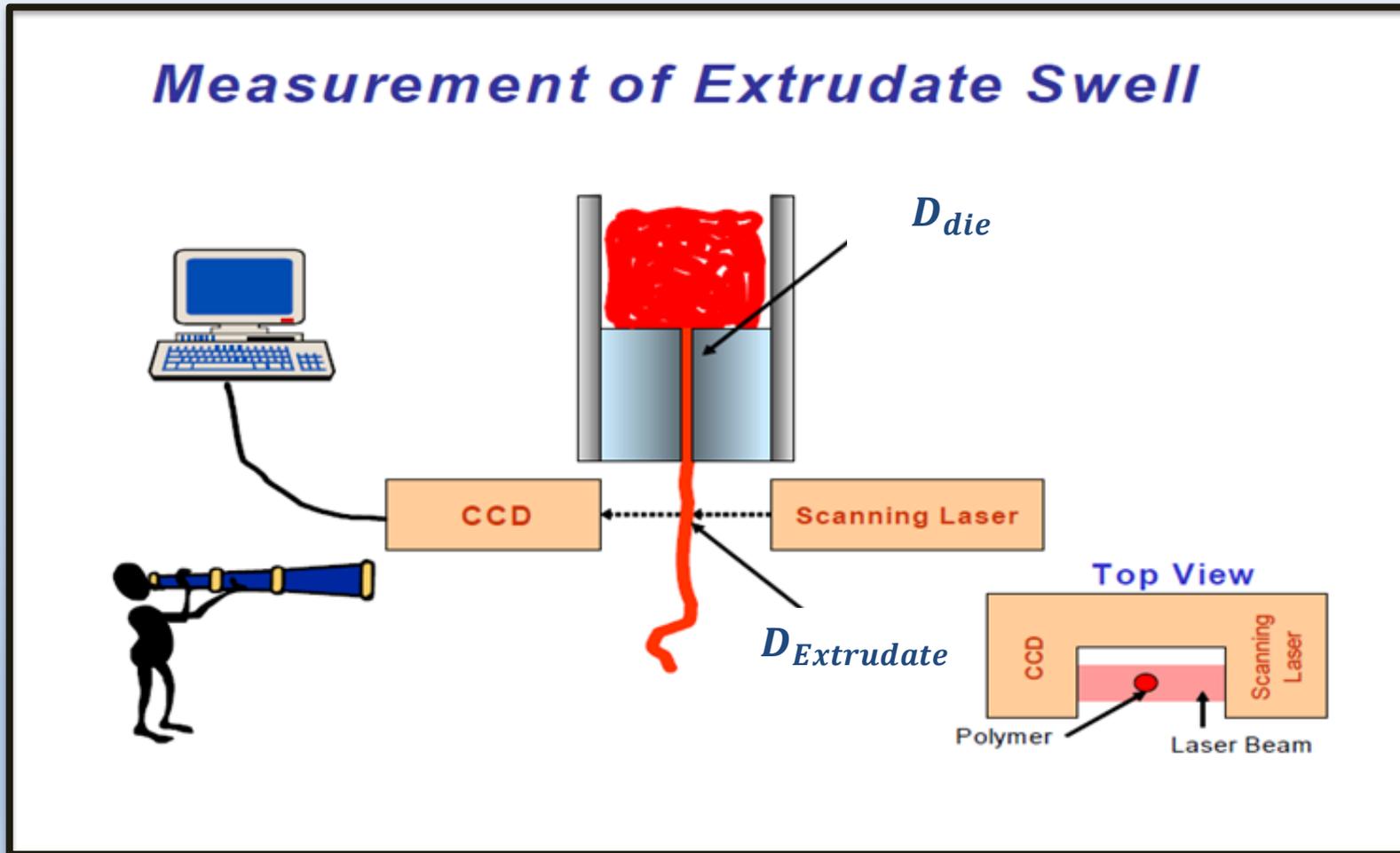


<https://www.azom.com>

$$\text{Percent die swell} = \frac{D_{Extrudate} - D_{die}}{D_{die}} \times 100$$

- ❖ Expansion (re-coiling) of extrudate after exiting die.
- ❖ Qualitative measure of melt elasticity.
- ❖ Relaxed die swell is used to predict part dimension
- ❖ Running die swell is used to predict productivity of extrusion process.
- ❖ Analysis of extrudate smoothness.
- ❖ Trouble shooting by using larger die diameter, longer die, tapering the die, lower shear rate, or higher temperature.

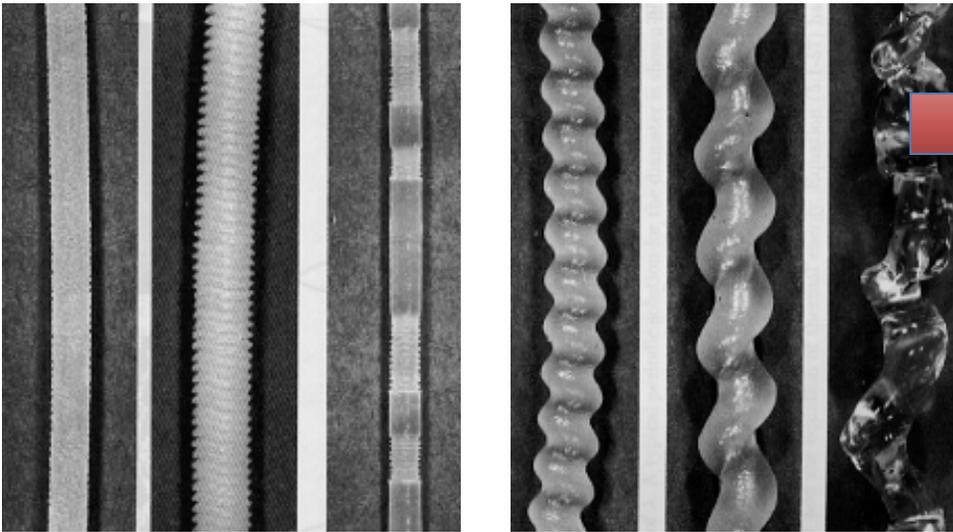
# Die Swell Measurement in LCR



- ❖ Detection: CCD element
- ❖ Light source: 800 nm laser
- ❖ Resolution: 2.75  $\mu\text{m}$
- ❖ Measuring range: 0.13-23 mm
- ❖ Response time: 1.4 ms
- ❖ Accuracy:  $\pm 0.003$  mm

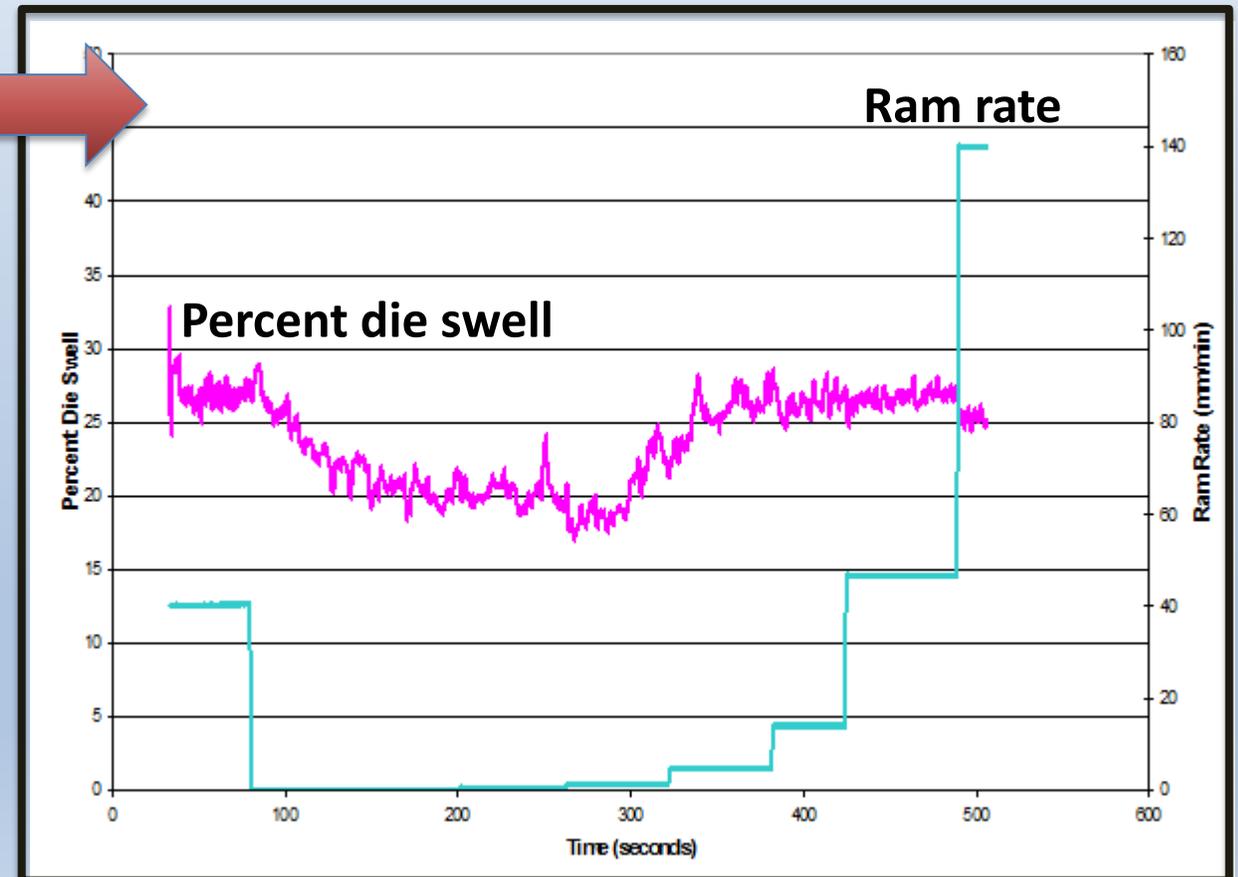
# Die Swell Measurement in LCR

## Melt Fracture

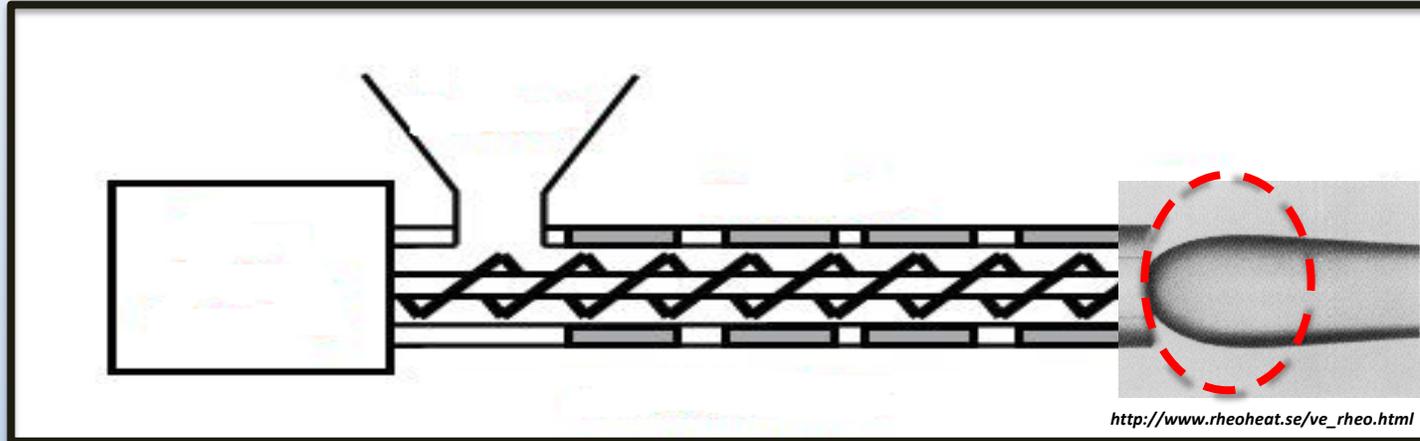


<https://www.azom.com/article.aspx?ArticleID=13578>

Melt fracture produce a noisy die swell measurements.



# Die Swell Trouble Shooting in Extrusion Process



This phenomena happens due to elasticity of polymer melts. **Any procedure that reduces the melt elasticity will help to troubleshoot.** e.g.:

- ✓ Increasing temperature
- ✓ Reducing screw speed (shear rate)
- ✓ Increasing the die length or die diameter
- ✓ Tapering the die



From lab to production,  
providing a window into the process



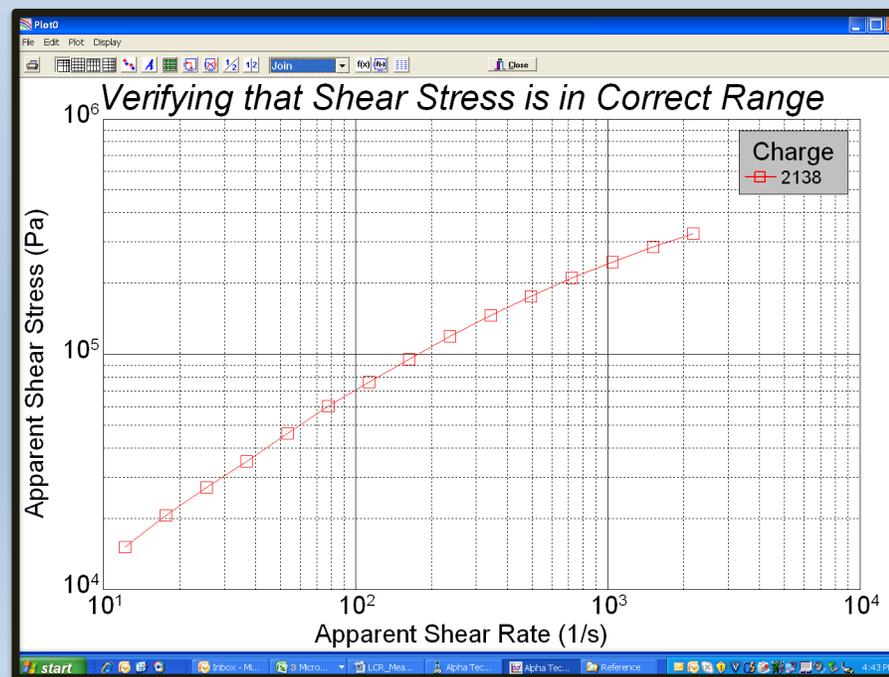
# MFR Correlation

# How to Calculate MFR from Capillary Rheometer?

1. Calculate the shear stress in the melt flow rate tester (using a standard die)

Weight in MFR test (kg)	Shear stress (Pa)
2.16	19350
5.00	44792
10.00	89584
21.60	193502

2. Determine the shear rate achieved at this shear stress from material flow curve



# How to Calculate MFR from Capillary Rheometer?

3. Calculation of melt volume rate (MVR) as follow:

$$MVR = 600\dot{\gamma} \frac{\pi R^3}{4}$$

where

- $MVR$  ( $cm^3/10min$ ): Melt volume rate
- $\dot{\gamma}$  ( $\frac{1}{s}$ ): Shear rate determined at “step 2”
- $R$  ( $cm$ ): Standard melt flow rate tester die radius

4. MFR calculation knowing polymer melt density as follow:

$$MFR = MVR \times \rho_m$$

where

- $\rho_m$  ( $\frac{g}{cm^3}$ ): Polymer melt density

# How to Measure MFR in LabKars?

The screenshot shows the 'Dynisco Polymer Test - Analyze' software interface. The 'Interpolate' button in the top toolbar is circled in red. A red box highlights the 'Melt Flow' section at the bottom, which includes dropdown menus for 'Load' (set to 2160) and 'Melt Density' (set to 0.75), along with 'MVR cc/10min' (0.143) and 'MFR g/10min' (0.107). The 'Coefficients in Polynomial' dropdown is set to 3. The 'Melt Flow' section is annotated with a red box and an arrow pointing to the text: 'Insert "Load" in g and polymer "Melt Density" in g/cm<sup>3</sup> in "Melt Flow" section'. The 'Interpolate' button is annotated with an arrow pointing to the text: 'Select "Interpolate"'. The 'Coefficients in Polynomial' dropdown is annotated with an arrow pointing to the text: 'Set "Coefficient in Polynomial" as 3'. The 'Melt Flow' section is annotated with an arrow pointing to the text: 'Insert "Load" in g and polymer "Melt Density" in g/cm<sup>3</sup> in "Melt Flow" section'. The 'Melt Flow' section is annotated with a red box. The 'Melt Flow' section is annotated with a red box. The 'Melt Flow' section is annotated with a red box.

**Select "Interpolate"**

**Set "Coefficient in Polynomial" as 3**

**Insert "Load" in g and polymer "Melt Density" in  $g/cm^3$  in "Melt Flow" section**

Rate (1/s)	Calc. Visc. (Pa-s)	Calc. Stress (Pa)
100	2154.1	215411.0
200	1319.3	263867.0
500	673.2	336578.0
1000	397.1	397091.0
2000	230.5	460964.0
5000	109.5	547867.0
10000	61.2	612323.0

Load	Melt Density	MVR cc/10min	MFR g/10min
2160	0.75	0.143	0.107

# How to Measure Melt Density in LCR?

Select  
"Position"  
Test Type

**Data Point Setup # 324**

Setup #	Program Name	Start Pos.	Temperature	Melt Time	Sensor1 ID	Die
315	PE Stability II		100	190	300 LC-502N	CX394-30
316	PE Short		100	190	300 LC-502N	CX394-30
317	PE Long		100	190	300 LC-502N	CX394-30
318	PE Slip Small		100	190	300 LC-502N	CX394-30
319	PE Slip Large		100	190	300 LC-502N	CX394-30
320	PP Sweep		100	190	300 LC-502N	CX394-30
321	PP Stability		100	190	300 LC-502N	CX394-30
322	PE Stability		100	190	300 LC-103N	CZ394-20
323	PE Shear Rate Long		100	190	300 LC-103N	CZ394-20
324	Melt Density		120	190	300 LC-103N	CZ394-20

Point #	Speed Control	Shear Rate	Delay Sec	Time Min	Acquire At-mm
1	32.89	400.00			134.0
2	32.89	400.00	30		148.0
3	32.89	400.00	30		162.0
4	32.89	400.00	30		176.0
5	32.89	400.00	30		190.0

Control Mode:  Rate  Stress

Test Type:  Steady State  Position (Acquire At - mm)  Manual  Time Delay (Acquire At - sec)  Elapse Time (Acquire At - sec)  Relaxed Die Swell per zone

Minimum Speed: 0.03  
Maximum Speed: 650

Apply Max Packing Force:  Relaxed Die Swell Delay: [ ] sec. Average Readings:  [ ] points, over last [ ] sec.  
Melt Pause: 30 sec. Backup Distance: [ ] mm  
Barrel Diameter: 0.376 inch MACRO [ ] Estimate TestTime: 300 sec.

Manage the positions to  
have 14 mm of piston  
travel distance between  
points

Five measurements of melt density

Whenever the plunger is  
in its delay time, cut the  
extrudate and weigh it



*From lab to production,  
providing a window into the process*



# Intrinsic Viscosity of PET

# What is Intrinsic/Solution Viscosity (IV)?



❖ Creating a dilute solution of the polymer and comparing the flow rate of the solution to the flow rate of the pure solvent

❖ **Advantages**

- Performing at room temperature
- No need to melt the polymer
- No need to dry hygroscopic polymers (e.g. PET, PA)
- Common flowability specification (rather than MFR) among the manufactures of hygroscopic and filled polymers

❖ **Disadvantages**

- Delicate apparatus
- Using of noxious chemicals as solvent
- Not environmental friendly

# Relationship between Melt Viscosity and Intrinsic Viscosity

**Melt viscosity**

$$\eta_{melt} \propto M_w$$

**Fox-Flory  
Equation**

$$\eta_0 = K_1(M_w)^{3.4}$$

$$\ln[\eta_0] = \ln K_1 + 3.4 \ln[M_w]$$

**Intrinsic viscosity**

$$\eta_{Intrinsic} \propto M_w$$

**Mark-Houwink  
Equation**

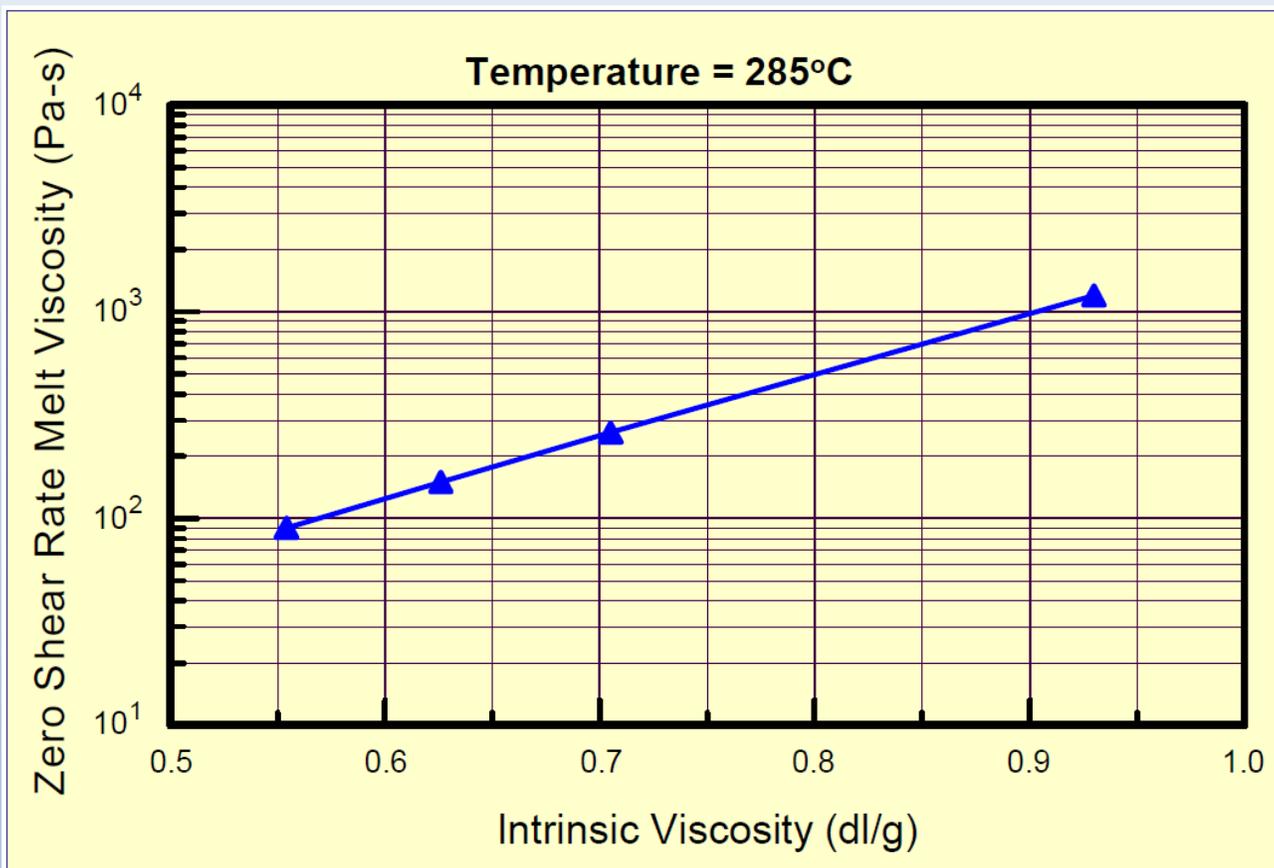
$$\eta_{Intrinsic} = K_2(M_w)^a$$

$$\ln[\eta_{Intrinsic}] = \ln K_2 + a \ln[M_w]$$

L.H. Sperling, *Introduction to Physical Polymer Science*, John Wiley & Sons, 4<sup>th</sup> Edition.

$$\ln[\eta_{Intrinsic}] = \frac{a}{3.4} \ln[\eta_0] + K''$$

# PET Melt Viscosity Versus Intrinsic Viscosity



$$\ln[\eta_{Intrinsic}] = \frac{a}{3.4} \ln[\eta_0] + K''$$

Slope:  $\frac{a}{3.4}$   $\longrightarrow$  For PET:  $a=0.75$

Intercept:  $K''$

# How to Determine IV of PET in LCR Capillary Rheometer?

Dynisco Polymer Test - Analyze

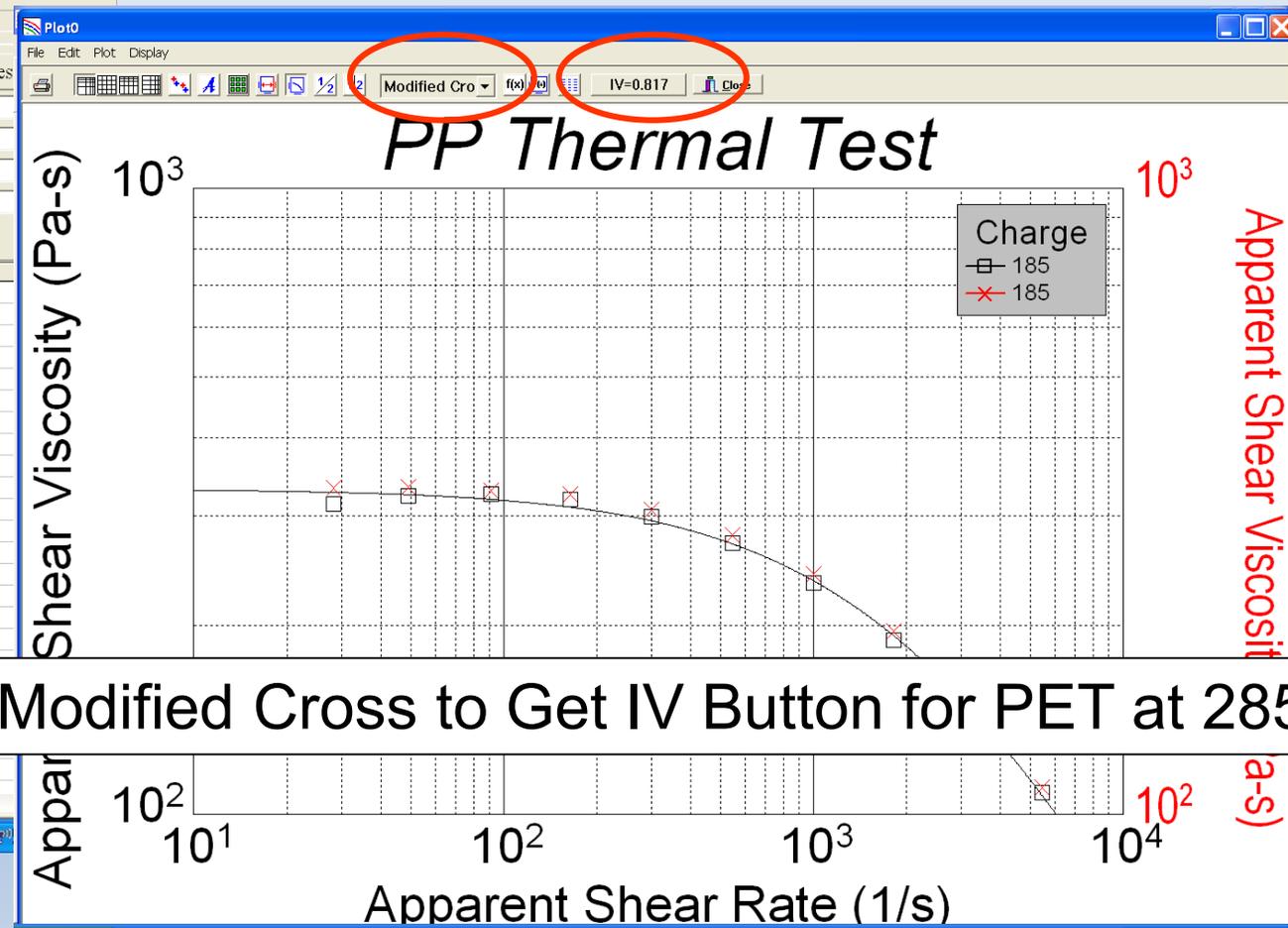
Database Path: d:\PROGRA~1\LABKAR~2\Database

Selected Charges: Global Preferences

Global Preferences dialog:

- Reference Point #1: I.V. 1.026 dl/g
- Reference Point #2: I.V. 0.650 dl/g
- Viscosity: 615.0 Pa-s
- Viscosity: 178.0 Pa-s
- Slope: 0.215
- Offset: 2.36

Program	Charge	DateTime	Sample	Temperature	Comment
FMC	1248	08/31/2007 02:3	HDPE	-1	210 Test Config 2
FMC	1249	09/04/2007 01:5	HDPE	-1	210 Test Config 2
FMC	1250	09/04/2007 02:5	HDPE	-2	210 Test Config 2
FMC	1251	09/04/2007 04:2	HDPE	-2	210 Test Config 2
FMC	1252	09/05/2007 08:3	HDPE	-2	210 Test Config 2
FMC	1253	09/05/2007 09:4	HDPE	-2	210 Test Config 2
FMC	1254	09/05/2007 10:3	HDPE	-2	210 Test Config 2
FMC	1255	09/05/2007 11:5	HDPE	-2	210 Test Config 2
FMC	1256	09/05/2007 01:4	HDPE	-2	210 Test Config 2
FMC	1257	09/05/2007 02:5	N 2.5	-2	210 Test Config 2
FMC	1258	09/05/2007 04:3	LDPE	-2	210 Test Config 2
FMC	1259	09/05/2007 05:2	LDPE	-2	210 Test Config 2
FMC	1260	09/06/2007 09:1	LDPE	-2	210 Test Config 2
FMC	1261	09/06/2007 01:1	LDPE	-2	210 Test Config 2
FMC	1262	09/06/2007 01:5	2.5 N	-2	210 CX394-20, CX394-20
FMC	1263	09/06/2007 03:5	2.5 N	-2	210 CX394-20, CX394-20
F2MC	1264	09/07/2007 09:1	2.5 N	-2	210 CZ787-15, CZ787-15
F2MC	1265	09/07/2007 03:4	2.5 N	-2	210 CZ787-1, CZ787-1
F2LR	1266	09/07/2007 04:1	2.7 N	-2	210 CZ787-1, CZ787-1
F2LR	1267	09/10/2007 08:5	2.7 N	-2	210 CZ787-1, CZ787-1
F2LR	1268	09/10/2007 09:3	2.7 N	-2	210 CZ787-1, CZ787-1
F2LR	1269	09/10/2007 10:0	2.5 N	-2	210 CZ787-1, CZ787-1
F2LR	1270	09/10/2007 10:3	2.5 N	-2	210 CZ787-1, CZ787-1



Use Modified Cross to Get IV Button for PET at 285 C



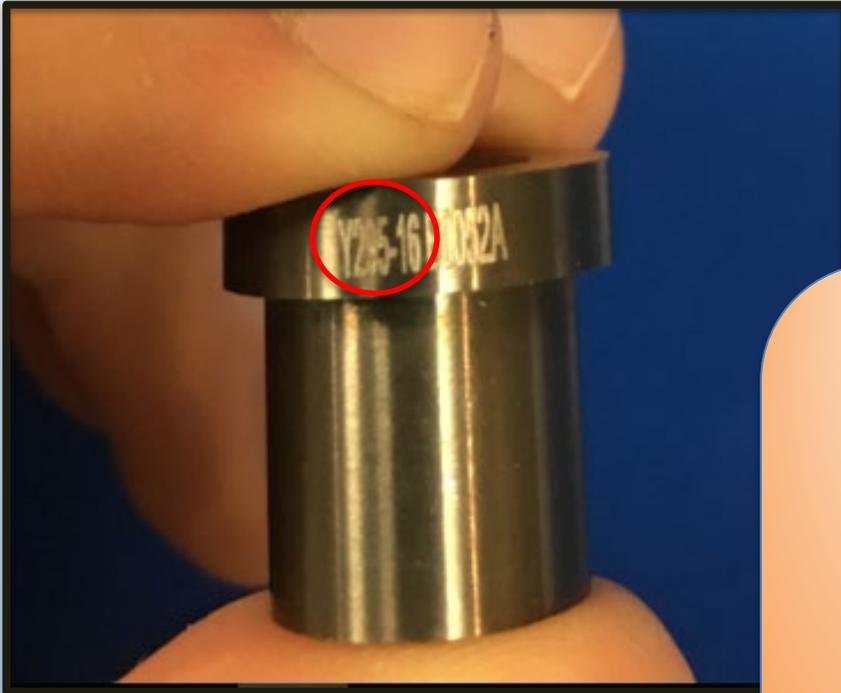


From lab to production,  
providing a window into the process



# LCR Dies Information

# LCR Die Part Number Code



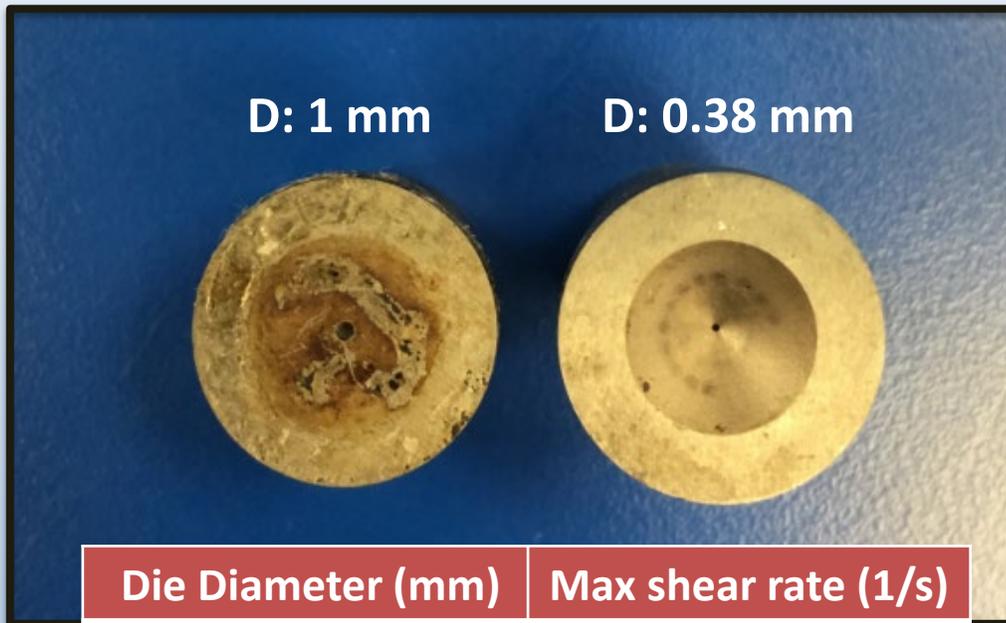
Formula for die part number:

**ADDD-LL**

where

- A: entry angle  
(W=60°, Y=90°, X=120°, Z=180°)
- DDD: diameter in inches×10000
- LL: length to diameter ratio

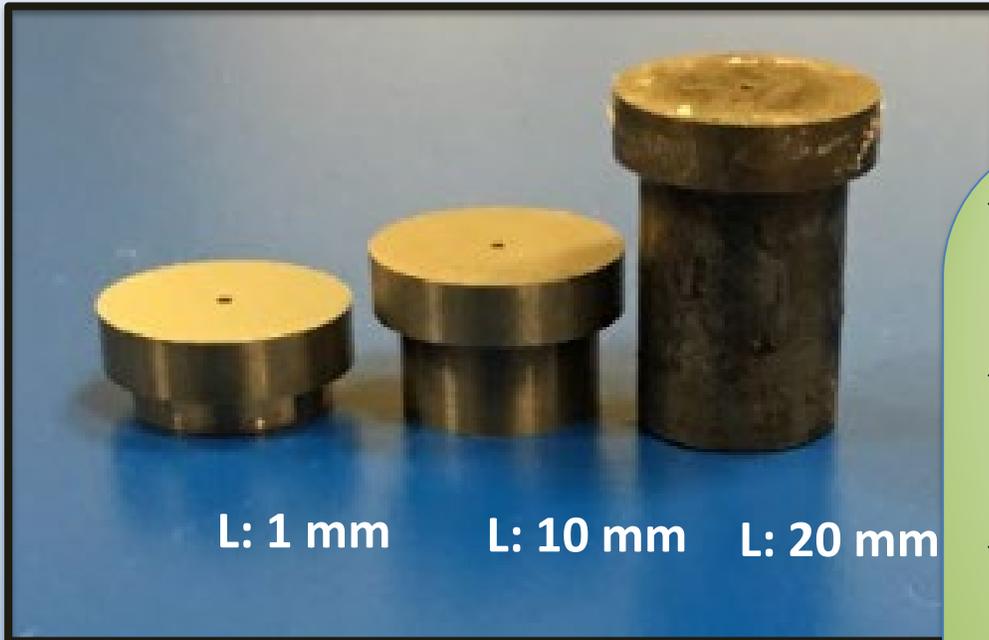
# Die Diameter



Die Diameter (mm)	Max shear rate (1/s)
0.38	142000
0.75	18700
1.00	7900
1.50	2300
2.00	980

- ❖ Smaller diameter produces higher shear rates.
- ❖ Larger diameter causes less elastic deformation applied at the entrance of the die.
- ❖ larger diameter cause less entrance pressure drop, less die swell, less extensional deformation, and less slippage.
- ❖ For calculation of wall slip velocity at least 2 dies with different diameters (same L/D) are required.

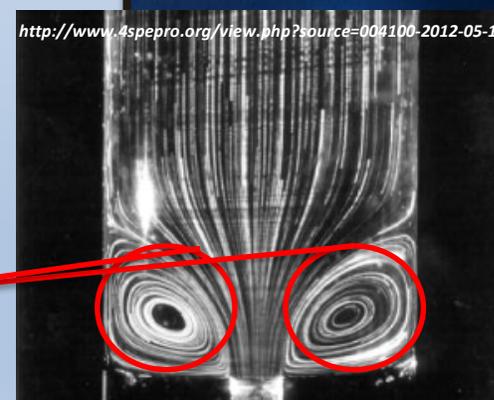
# Die Length



- ❖ The portion of fully developed flow in compare with entrance region increases with increasing the die length
- ❖ The percent error produced by entrance region is less with longer die.
- ❖ Short die for measuring elastic deformation (e.g. die swell, slippage) and long die for measuring shear viscosity.
- ❖ Noisy reading from short die at very low shear rates
- ❖ For calculation of entrance pressure (Bagley correction) and extensional viscosity, at least 2 dies with different L/D ratio (same diameter) are required.

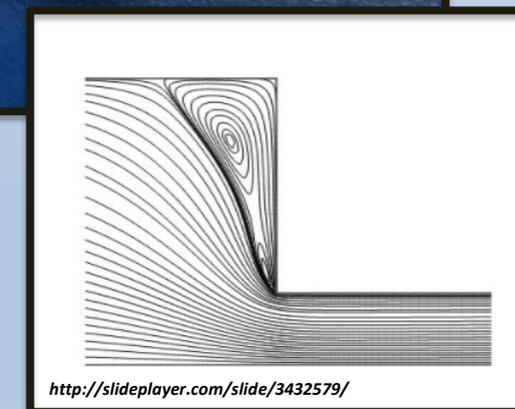
# Die Entrance Angle

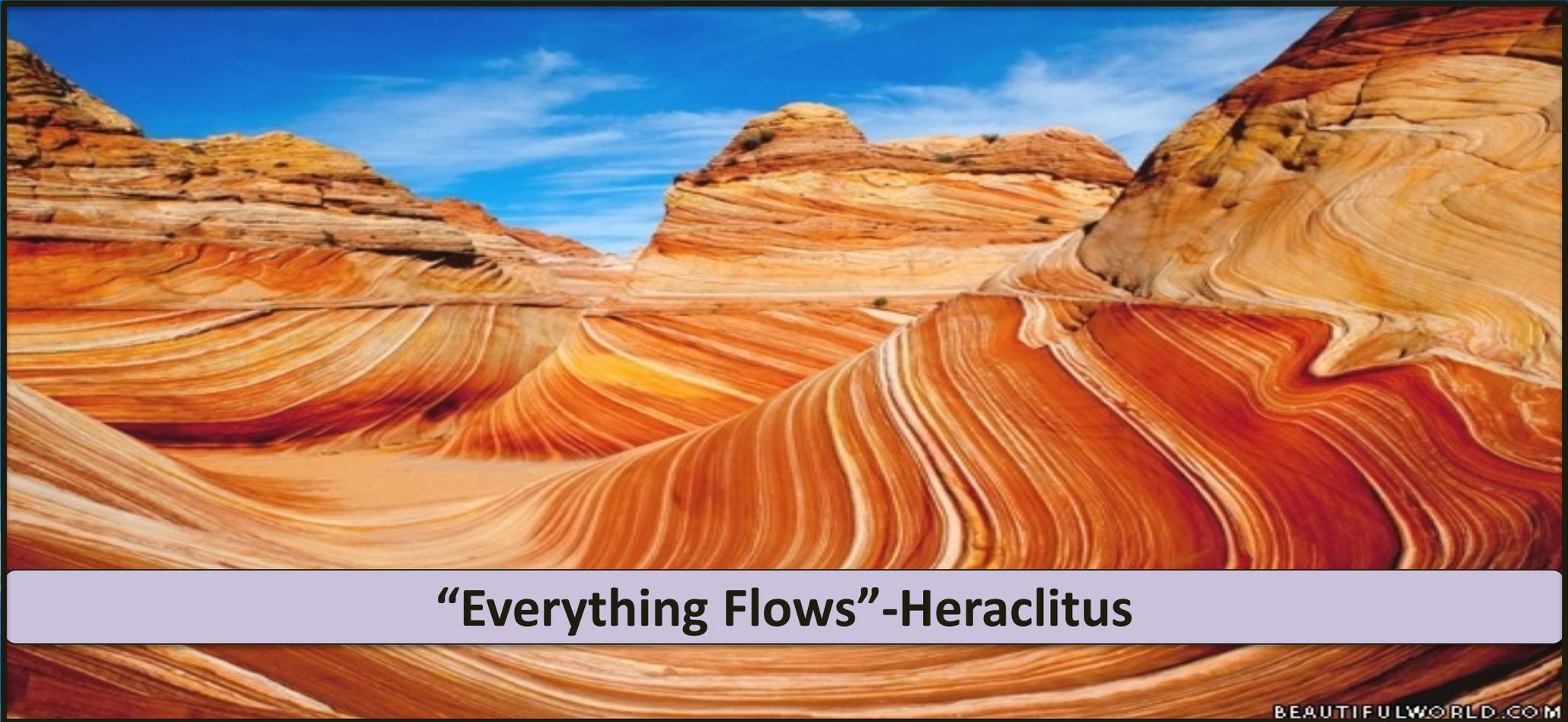
- ❖ Entrance angle has effect on flow patterns at the entrance to the capillary die.
- ❖ Lower angle causes smoother flow, less vortex flow, and less energy consumption at the die entrance.
- ❖ Lower angle reduces the elastic deformations (e.g. less entrance pressure drop, extensional deformation, die swell, melt fracture and wall slippage).
- ❖ Lower angle favors shear flow.



**Stationary vortex flows  
in the corner region**

**Flow pattern at the entrance to  
a die with a flat entrance (180°)**





**“Everything Flows”-Heraclitus**

BEAUTIFULWORLD.COM

**QUESTIONS ?**